

Resistive core, moment inertia  $\Theta$ ,  $S$  top month + assumed  
 $S = S(r) \Rightarrow$  static. E., Billard, p. 89

From Lyttleton,  $k_s = \frac{1}{S} \left( \frac{\partial S}{\partial p} \right)_s = \frac{1}{a+b p}$

$$\therefore \frac{\partial S}{\partial r} = \left( \frac{\partial S}{\partial p} \right)_s \left( \frac{\partial p}{\partial r} \right) = -k_s S^a g$$

$$= -\frac{S^a}{a+b p} g$$

$$k = \frac{1}{S} \frac{\partial S}{\partial p} = \frac{1}{a+b p}$$

$$\therefore \frac{\partial S}{S} = -\frac{\partial p}{a+b p}$$

Set  $x = a+b p$ ,  $dx = b dp$

$$\frac{dg}{S} = -\frac{dx/b}{x} = \frac{1}{b} \frac{dx}{x}$$

$$\int \frac{\partial S}{S} = \frac{1}{b} \int \frac{dx}{x}$$

$$\ln \frac{S}{S_0} = \frac{1}{b} \ln \left( \frac{x}{x_0} \right) = \frac{1}{b} \ln \left( \frac{a+b p}{a+b p_0} \right)$$

$$\frac{S}{S_0} = \left( \frac{a+b p}{a+b p_0} \right)^{\frac{1}{b}}$$

$$\left( \frac{S}{S_0} \right)^b = \frac{a+b p}{a+b p_0}$$

But  $p_0 \approx 0$ .

$$\left( \frac{S}{S_0} \right)^b = 1 + \frac{b}{a} p$$

$$\boxed{p = \frac{a}{b} \left\{ \left( \frac{S}{S_0} \right)^b - 1 \right\}}$$

Very roughly,  $a = 1.5 \times 10^{12}$  degrees cm<sup>-2</sup>  
 $b = 3.5$  (dimensionless)

For density at  $\oplus$  center,

$$\frac{S}{S_0} = \left(1 + \frac{b}{a} p\right)^{\frac{1}{b}} = \left(1 + \frac{3.5 \times 3.6 \times 10^{12}}{1.5 \times 10^{12}}\right)^{\frac{1}{3.5}}$$

$$= (1 + 8.4)^{\frac{1}{3.5}} = (9.4)^{\frac{1}{3.5}} \approx 1.9$$

For  $S \approx 17 \text{ g cm}^{-3}$  and  $S_0 \approx 6 \text{ g cm}^{-3}$  according to Sodalis,  
whereas Fe has  $7.9 \text{ g cm}^{-3}$   
Mass very low in the Sun  
But p might be slightly larger.

~~$$\rho = \frac{a}{b} \frac{d}{dr} \left(\frac{S}{S_0}\right)^b - 1$$

$$= \frac{a}{b} d \left(\frac{S}{S_0}\right)^{b-1} \frac{dS}{dr} = a \left(\frac{S}{S_0}\right)^{b-1} \frac{dS}{dr}$$

$$= \text{and } \frac{dS}{dr} = \text{constant}$$~~

$\rho = \frac{a}{b} \frac{d}{dr} \left(\frac{S}{S_0}\right)^b$  for a homog. sphere.

~~$$\therefore \frac{S}{S_0} \frac{r}{R} = a \left(\frac{S}{S_0}\right)^{b-1} \frac{dS}{dr}$$

$$\therefore \frac{S_0 S_0}{a R} \frac{r}{r_0} \frac{dS}{dr} \approx \left\{ \begin{array}{l} S^{b-2} \frac{dS}{dr} \\ S^{b-1} \end{array} \right.$$

$$\frac{dS}{dr} = \sqrt{\frac{S_0^2}{a R} \frac{r}{r_0}}$$~~

Could attempt hydrostatic equl.  $\rightarrow$  diff. of  
boxed eq., but only know  $g = g_0 \frac{r}{R}$  for  
homog.  $\oplus$ .

Core densities are  $10 - 17 \text{ g cm}^{-3}$ ,  $\therefore$  uncompacted  
core densities are  $5.2 - 9 \text{ g cm}^{-3}$ . Fe uncon-  
pressed is  $7.9 \text{ g cm}^{-3}$ .  $\therefore$  argument for Fe core,  
But some people (Rosen, Slichter) claim better  
model accuracy  $\rightarrow$  a discrepancy).

Comp. core. Seism. data. P + S waves.

$$\frac{\partial \chi}{\partial p} = v_p^{-2} - \frac{4}{3} v_s^{-2} \text{ from theory of elastic}$$

wave propagation. Seismographic frequency + amplification  
ranges. Fast mode oscillations  $\oplus$  in  $P \propto \frac{1}{\sqrt{V_S}}$ ,  $\sim 1 \text{ hr.}$

Reflec., refrac. Birch Fig. 2. Discords.  $\Rightarrow$

phase or composition change. Val vs.  $p$  or  $S$

is a comp. index. Birch Fig. 3. + p. 135. Meteorites.

Core form: melting early, redundant later, gradual migration Fe to interior. Wenz. (notion, Bullard,

p. 102. Common vs. uncommon.

Pressures  $10'' - 4 \times 10^{12}$  dynes  $\text{cm}^{-2}$  too high for

Lab. + too low for theory (electron shells stripped)

Ref.: E. Segré, "Nuclei + Particles" Benjamin, N.Y.  
1965, pp. 37-38

A charged particle ionizes the gas it penetrates.  
Only part of the energy is used in ionizing  
& in producing suprathermal electrons; the  
remainder is used ~~the~~ in molecular excitation  
leading to emission of radiation. The avg. ~~an~~  
energy required per ion pair is "remarkably  
independent of the charge, mass, & velocity  
of the particle producing the ionization, but  
depends on the gas in which the ion is formed."

Some of the suprathermal electrons (delta rays)  
have sufficient energy to produce secondary ions.

eV/ion pair

He Ne Ar Xe H<sub>2</sub> O<sub>2</sub> N<sub>2</sub> CO<sub>2</sub> Air

42.7 36.8 26.4 21.9 36.3 32.5 36.5 34.3 35.0 Po  $\alpha$

42.3 36.6 26.4 22.0 36.3 30.9 31.9 32.9 33.8 H<sup>3</sup>  $\beta$

... except for He, Ar, Xe, all others have ~ 34 eV/ion

pair

This gives, further 2 plates,

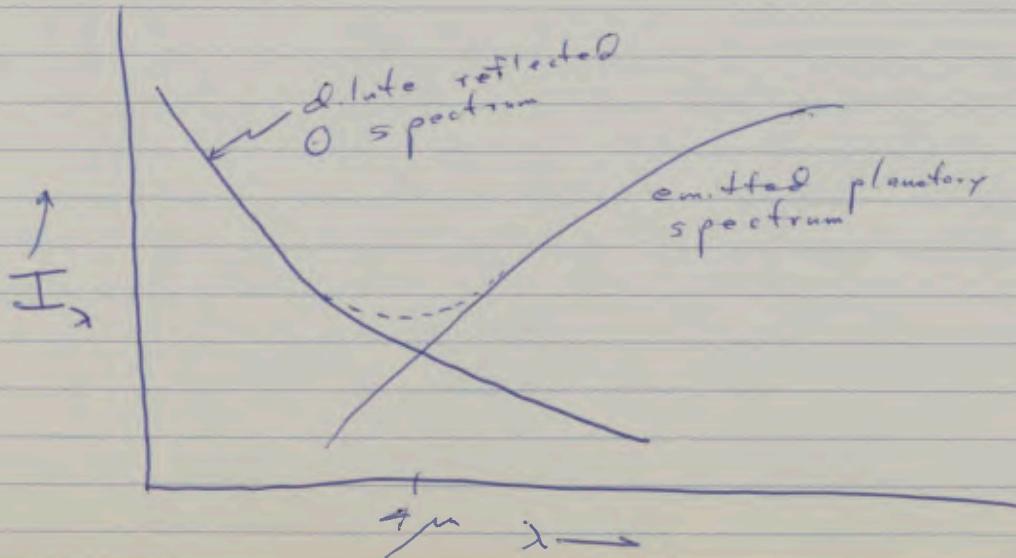
$$T_{\text{rot}} = 257^{\circ}\text{K} \quad + \quad T_{\text{rot}} = 434^{\circ}\text{K},$$

respectively. The pressures depend somewhat on the choice of  $T$ . For  $\bar{T} = 22$ , the  $P$ 's are 1.8 and 5.6 atm, respectively.

Significance of results. High  $P \Rightarrow$  high  $T$ . Variable cover at 7830 Å. Determination of  $I_{\text{CO}_2}$ . Search for H<sub>2</sub>O. Poss. double maximum, suggesting 2 cloud layers.

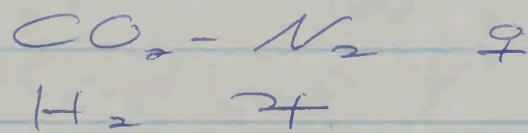
### Planetary temperatures:

Could be measured by determining the Wien peak, or by taking ratio of intensities at neighboring wavelengths. These methods do not depend on absolute calibrations, but they do require high-sensitivity detectors, since  $\lambda$ -intervals are used. In practice, absolute energy intensity determinations are used. Usually thermocouples or thermistors, & almost always in the 8 - 13 μ window. These temps are really brightness temps. Unless the sources are black gray bodies, measurements elsewhere might give diff. temps. E.g., for O<sub>2</sub>,



## Pressure-induced dipole transitions

Here line-width is a fraction of the time for establishing the transient dipole moment.  
∴ & a fraction of velocity, i.e., of  $T$ , alone,  
and independent of pressure. ∴  $\propto p^{1/2}$  —  
the usual Lorentz case is removed. — the  
shape of a pressure-induced line is pressure-  
independent at a fixed temperature. The  
absorption coefficient,  $k_r$ , on the other hand,  
is  $\propto p^2$ , because the number of emitters  $\text{cm}^{-3}$   
 $\propto p$ , and the number of stimulated  $\text{sec}^{-1}$  is  $\propto p$ .  
For pressure-induced transition, the collision  
time  $\ll$  time between collision.  $\Delta E \gg kT$   
 $\Rightarrow$  SE much larger. — pressure-induced transitions  
are very broad in the i.e., & almost continuous  
at microwave frequencies. At microwave frequencies  
it is translational rather than vibrational &  
rotational transitions which are occurring.



$\text{CH}_4$	$1.16, 1.7 \mu$	$< 10 \text{ cm-atm}$
$\text{C}_2\text{H}_4$	$1.68 \mu$	$< 2 \text{ cm-atm}$
$\text{C}_2\text{H}_6$	$1.20, 1.73 \mu$	$< 1 \text{ cm-atm}$
$\text{NH}_3$	$1.51 \mu$	$< 2 \text{ cm-atm}$

Downwards later

$\text{CH}_3\text{Cl}$  spectrum.

$$\bar{\nu} = \frac{1}{\lambda} = \text{cm} \frac{\nu}{\text{cm}}$$

Units of wave nos. or  $\text{cm}^{-1}$ .

Boltzmann distribution of states: if a sys. no. ( $N$ ) of particles are placed in a given potential well, how many will occupy which energy level, if the states are quantized? Answer given by the Boltzmann distri. which states that the no. parts. occupying a state w. energy  $E_i$  is related to the no. occupying some other state  $E_j$ , which has less energy, by

$$N_i = N_j e^{-(E_i - E_j)/kT}$$

Sometimes  $\exists$  several states with the same energy, i.e. degeneracy. The population of the energy level is then greater. Thus, if  $g_i$  is the multiplicity of the  $i$ th level, (i.e., no. states w. energy  $E_i$ ) and ( $\omega$  is usually the case) lowest energy level is a singlet state,

$$N_i = g_i N_0 e^{-(E_i - E_0)/kT}$$

$$\frac{N_i}{g_i} = \frac{N_0}{g_i} e^{-(E_i - E_0)/kT}$$

Pressure-induced: Permeated by later swollen atoms like dry

line with fracture of line for establishing

dipole moment  $\Rightarrow f(v) \Rightarrow f(T) \neq f(p)$ .

P dipole moment removed. : always pressure induced line

is p-induced at fixed T. Coll & coll between later cells.

$\Delta E$  ( $\Delta E$  str + t) bigger in p-induced film broad at  
it's widest = contain as many.

$k_{\text{coll}} \propto p^2$ . Nonlinear  $\propto p$ ; no straight line  $\propto p$ .  
 $\text{CO}_2 - \text{N}_2$   $\frac{1}{2}$ ;  $\text{H}_2 - \frac{1}{4}$ .

Atmos. branching  
mode = mobility  
(not rate or vel.)

Vibration of a single particle is given by the simple diff. eq.

$$m \ddot{x} = -kx,$$

where  $k$  is the force const. in units of dynes/cm.  
The sol. is

$$v = \frac{1}{2\pi} \sqrt{\frac{k}{m}}.$$

The potential energy is parabolic

$$U = \frac{1}{2} k x^2$$

if the equilib pos. is taken as the zero of potential energy.

Now consider 2 parts connected by a spring:

$$m_1 \ddot{x}_1 = -k(x_2 - x_1)$$

$$m_2 \ddot{x}_2 = -k(x_2 - x_1)$$

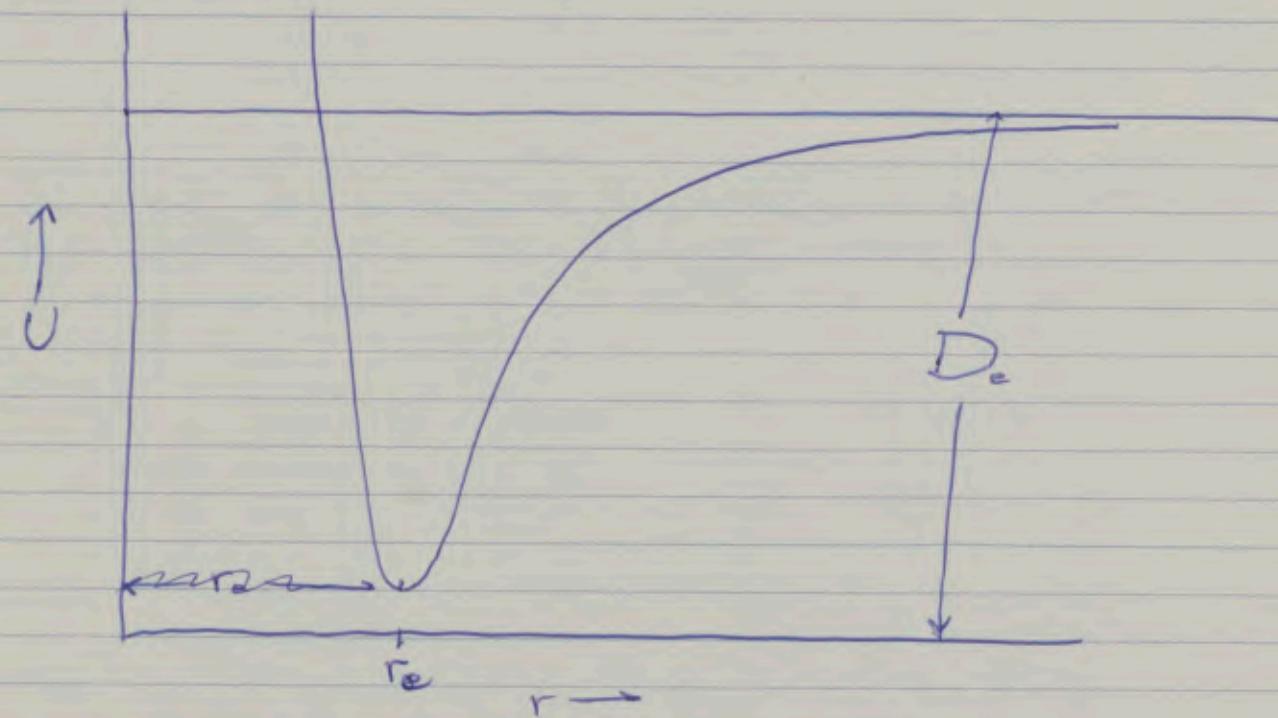
The sol. is

$$v = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}}$$

where  $\mu$  is the reduced mass, given by

$$\frac{1}{\mu} = \frac{1}{m_1} + \frac{1}{m_2}$$

Now for a diatomic mol., we are interested in the  $\Delta V$  as a function of the distortion of the bond of the molecule from its equil. distance. Except for  $H_2$ ,  $\exists$  no calc. of  $E = E(r)$  from the interactions between the bonding electrons + the atomic nuclei. The gen. shape of the pot. energy curve can, however, be sketched. One knows, e.g., that if a bond is stretched far enough it will break; i.e., mols. dissociate. Also, bonds strongly resist compression, as is revealed, e.g., by the rel. incompressibility of solids i.e., one expects



$r_s$  = equil. position,  $D_e$  = dissociation energy.

I am ad hoc analytic expression for this, the Morse pot.:

$$U(sr) = D_e \left(1 - e^{-\beta(s-r)}\right)^2$$

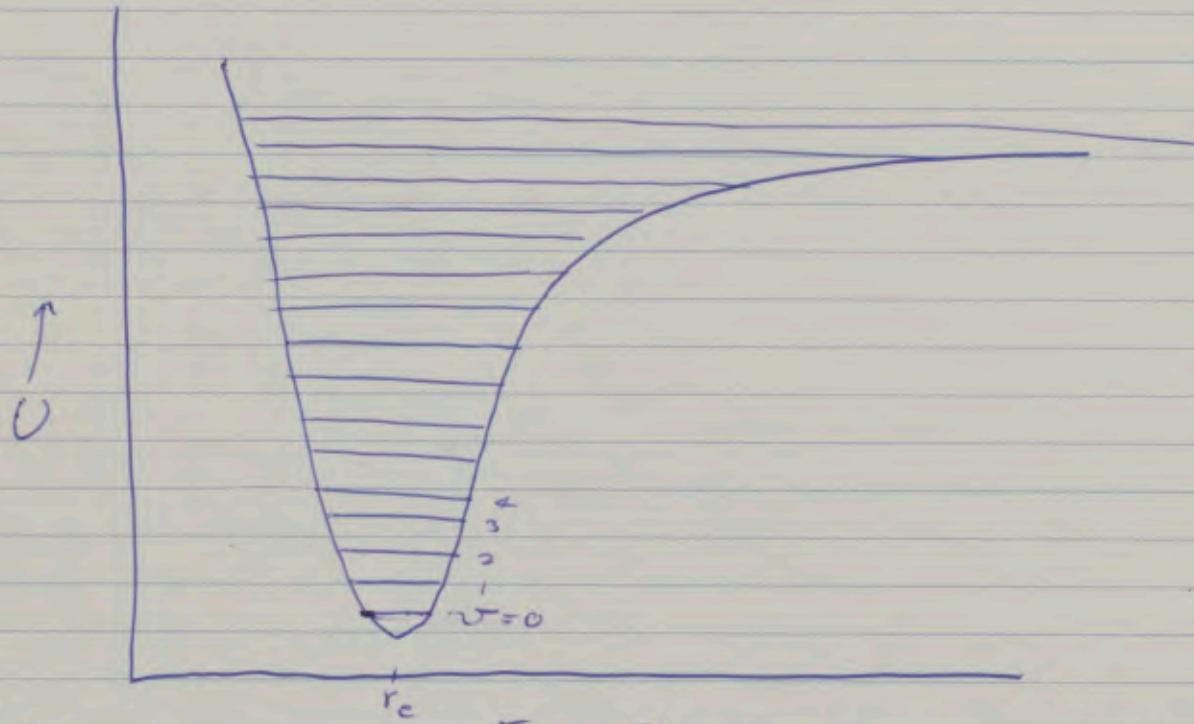
$\beta$  is a factor of the molec. species.

Now the q.m. sol. of the diatomic harmonic oscillator is

$$E_v = (v + \frac{1}{2}) \hbar \omega, \quad v=0, 1, 2, \dots$$

where  $\omega = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}}$ ,

i.e. the classical energy levels are quantized.  
Planck's  $E = h\nu$  is used, + a zero-ph. energy.



Equally spaced energy levels, each w. its own quantum no.  $v$ , & some value of  $v$  above which dissociation occurs.

3 restrictions on the vibrational transitions  
 which can occur. A vibrating molecule cannot interact w. c.m.rnd. unless an oscillating dipole moment accompanies the molecular vibration. Qualitatively, the oscillating dipole couples w. the  $\vec{E}$  field of the c.m.rnd. so energy can be exchanged between mol. + rnd. Turns out that homonuclear diatomic molecules have 0 dipole moment for all  $r$ ,  $\therefore$  have no vibrational spectra. Heteronuclear diatomic mols have  $p = p(r)$   $\therefore$  can absorb + emit energy by making vib. transitions among its vib. energy levels.

Even for these mols, 3 a further restriction, which is rigorously applicable only to harmonic oscillators, v.i.z,

$$\Delta v = \pm 1.$$

Now the energy spacing between vibrational energy levels is typically

$$\sim 2 \times 10^{-13} \text{ erg/molecule} \approx 3000 \text{ cal/mole.}$$

For  $g_1 = g_0 = 1$ , we compute no. mols in  $v=1$  state of mol. in  $v=0$  state at  $25^\circ\text{C}$ .

$$\frac{N_{v=1}}{N_{v=0}} = e^{\frac{-2 \times 10^{-13}}{299 \times 1.38 \times 10^{-16}}} = 0.008.$$

$\therefore$  less than 1% in  $v=1$ ; + even fewer in higher energy levels.  $\therefore$  in exp'ts not much above room temp. transition beginning in ground state dominates. If we find  $v=1$  ground state transits, we know something about temp.

♀?

There do exist hot bands, e.g. the CO<sub>2</sub> bands at 9.4 + 10.4 μ, which have much smaller ΔE + are excited at much higher T's. For ordinary ΔE, T ≥ v = 1, result is

$$\frac{2 \times 10^{-13}}{1.38 \times 10^{-16} \times T} \sim 2$$

$$T \sim \frac{100}{k \times 10^3} \text{ K}$$

at surfaces of O<sup>+</sup> + O<sup>-</sup> v=1 excitation just begins to become imp. But hot bands very imp. there.

Value of force const. k can be derived from one optical feature + used to derive others. E.g., HCP absorbs at 2890 cm<sup>-1</sup> = 3.47 μ.

$$\therefore \nu = 3 \times 10^{10} \times 2.89 \times 10^3 = 8.67 \times 10^{13} \text{ cycles/sec.}$$

$$\therefore \Delta E = h\nu = 6.62 \times 10^{-27} \times 8.67 \times 10^{13} \\ = 5.83 \times 10^{-15} \text{ erg.}$$

This must correspond to transition between v=0 + v=1; i.e.

$$\Delta E = \frac{\hbar}{2\pi} \sqrt{\frac{k}{\mu}}$$

$$\mu \approx m_H$$

$$\therefore k = 4.8 \times 10^5 \text{ dynes/cm.}$$

Then one derives high T excitation bands originally.  
The k's are a measure of bond strength.  
E.g.,

$H_2$	$5.0 \times 10^5$ dynes/cm
$CO$	18.7
$O_2$	11.4
$N_2$	22.6
$NaCl$	1.2

Actually, the harmonic oscillator has  
expression

$$V = \frac{1}{2} k (4r)^2$$

is only an approximate representation. It is observed that weak overtone absorption features exist corresponding to  $\Delta v = +2, +3, \dots$ . Also these overtone absorption are not exactly  $2, 3, \dots$  times the frequency of the Fundamental  $\Delta v = +1$  absorption. Very roughly intensity of overtones  $\sim 1\%$  intensity fundamental.

Refs.: G. Herzberg, Spectral Distortion Mols., 1950  
Infrared + Raman Spectra, 1945  
both in Norstrand

W. Brügel, Intro. to Mol. Spectroscopy,  
Wiley, 1963

G. Barro, Intro. to Mol. Spectroscopy  
McGraw-Hill, 1963.

B. Bak, Elementary Intro to Mol. Spectro  
Krell-Holland, 1962.

We now consider rotation of a linear diatomic molecule, although the theory developed is equally applicable to linear polyatomic mols, e.g.,  $\text{CO}_2$ , +  $\text{C}_3\text{O}_2$ . We will assume that rot. is uncoupled w. vibrat.; i.e., the rigid-rotor approximation.

To see simply how the physics proceeds we simply apply Bohr's fundamental condition that the ang-mom be quantized - units of

$$\hbar = h/2\pi.$$

Total ang-mom. is  $\rightarrow$  distance from cm.

$$\sum_m m \cdot v_i r_i = \sum_m m \cdot r_i^2 \left(\frac{v_i}{r_i}\right) = I \omega$$

where  $I = \sum_m m \cdot r_i^2$  is the moment of inertia of the system. Calling the rot. quantum no  $J$ , we have

$$I \omega = J \hbar, \quad J = 0, 1, 2, \dots$$

$\therefore$  the allowed energy levels are

$$E_J = \frac{1}{2} I \omega^2 = \frac{\frac{1}{2} (J \hbar)^2}{I}$$

$$= \frac{1}{2I} \hbar^2 J^2$$

$$E_J = \frac{\hbar^2}{8\pi^2 I} J^2$$

The correct eq., obtained by sol. of the Schrödinger eq. is only slightly diff.

$$E_J = \frac{\hbar^2}{8\pi^2 I} J(J+1).$$

∴ the ang. momenta are given by  $\sqrt{J(J+1)} \hbar$ , where  $J$ 's are integers. For spectroscopic work, it is convenient to express the energy levels in terms of wave numbers:

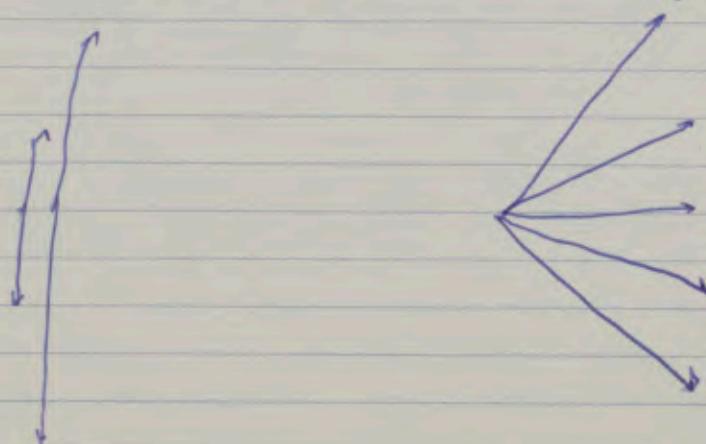
$$\tilde{E}_J = \frac{\hbar}{8\pi^2 c I} J(J+1) \text{ cm}^{-1}.$$

$$= \tilde{B} J(J+1) \text{ cm}^{-1},$$

where  $\tilde{B} = \frac{\hbar}{8\pi^2 c I} \text{ cm}^{-1}$

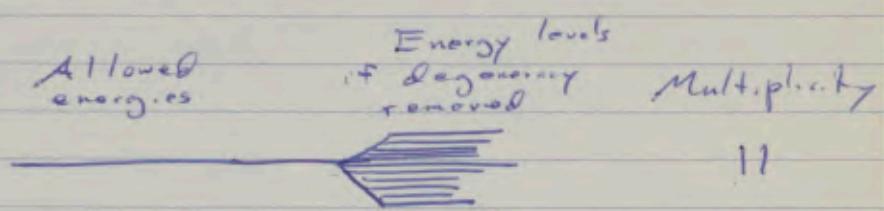
is a frequently occurring const. in mole spectroscopy.

Now if there are  $J$  no. of rot. states corresponding to a given rot. energy  $E_J$ . Since <sup>components of</sup> ang. mom. in a given direction are quantized in units of  $\hbar$ , there are  $2J+1$  states w. energies  $\tilde{B} J(J+1)$  e.g.,

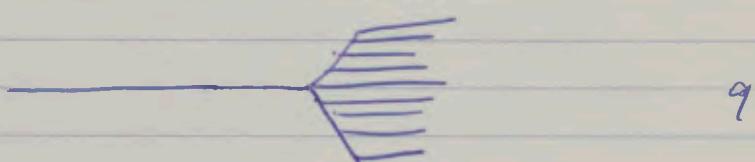


This  $2J+1$ -fold degeneracy of the  $J$ th energy level results in energy level diagram of the form

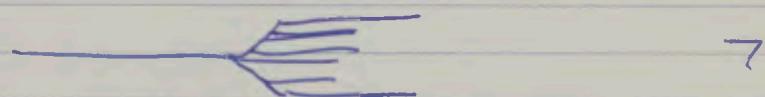
$$J \quad \tilde{E}_J \quad 5 \quad 30\bar{B}$$



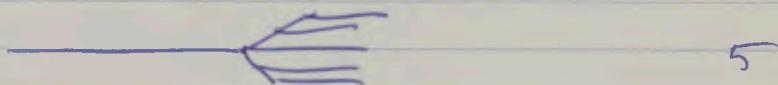
$$J \quad \tilde{E}_J \quad 4 \quad 20\bar{B}$$



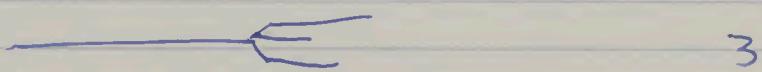
$$J \quad \tilde{E}_J \quad 3 \quad 12\bar{B}$$



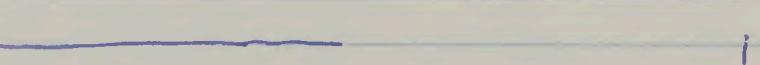
$$J \quad \tilde{E}_J \quad 2 \quad 6\bar{B}$$



$$J \quad \tilde{E}_J \quad 1 \quad 2\bar{B}$$



$$J \quad \tilde{E}_J \quad 0 \quad 0\bar{B}$$



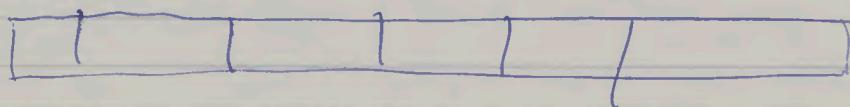
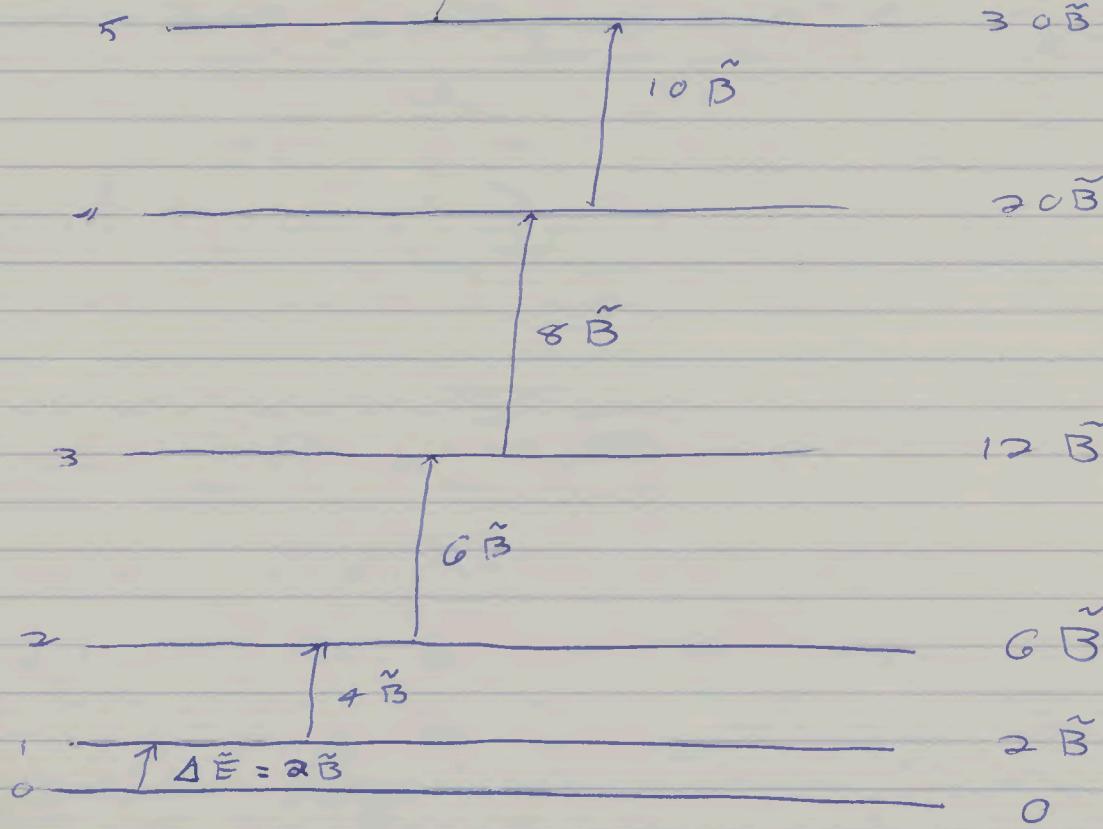
$$\tilde{\omega} = \tilde{B} J(J+1) \text{ cm}^{-1}, \text{ where } \tilde{B} = \frac{\hbar}{8\pi^2 c I} \text{ cm}^{-1}$$

$\Delta J = \pm 1.$

$\therefore$  a transition is

$$\begin{aligned}\tilde{\omega} &= \tilde{B} (J+1)(J+2) - \tilde{B} J(J+1) \\ &= 2\tilde{B} (J+1).\end{aligned}$$

$\therefore$  rot. lines are spaced by an amount  $2\tilde{B}$ .



$$\tilde{B}(J+1)[J+2-J]$$

Characteristic frequency is then

$$\tilde{\omega} = 2 \tilde{B} (J+1)$$

$$= 2 \frac{\hbar}{8\pi^2 c I} (J+1)$$

$$= \frac{2 \times 6.62 \times 10^{-27} \times 15}{8\pi^2 \times 3 \times 10^8 \times 3 \times 10^{-39}}$$

$$= 2.8 \times 10^1 = 28 \text{ cm}^{-1}$$

$$\therefore \lambda = \frac{c}{\tilde{\omega}} = 3.6 \times 10^{-2} \text{ cm. Typical microwave frequency}$$

Easy to see that microwave lines of  $\lambda \gg 1 \text{ cm}$  are not to be expected. This is, even better, a method of determining  $I$ .

Stretching effect of the centrifugal force on bond lengths + - or moment of inertia change the spectra; increase  $I$  + - decrease  $\tilde{\omega}$ . More mass for higher  $J$ 's.

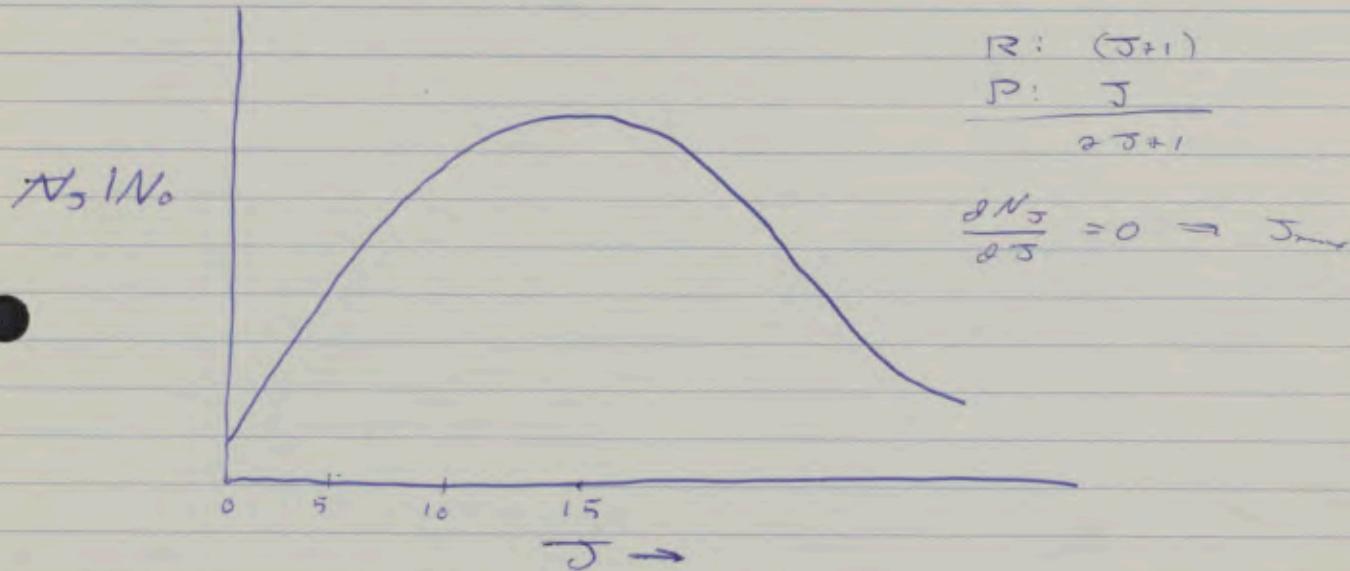
∴ from Boltzmann eq. -

$$N_J = (2J+1) N_0 e^{-B J(J+1)/kT}$$

Order of mag. I is  $\mu m_n \times (1\text{A})^2 \sim 10^{-38} \text{ g cm}^{-2}$ .

$$\therefore N_J = (2J+1) N_0 e^{-J(J+1) \times 2.0 \times 10^{-3}}$$

∴ at rm. temp.,  $\exists$  rel. pop. distrib like



As  $\alpha. J$  increases because of  $2J+1$ . At lg.  $J$  decreases bcs of exponential.

Here again  $\exists$  restrictions on permissible transitions. Here also the mol. must have a permanent d.pole moment. [EPassw.-induced transitions] Also  $\exists$  the selection rule

$$\Delta J = \pm 1.$$

## Vibration of polyatomic mols.

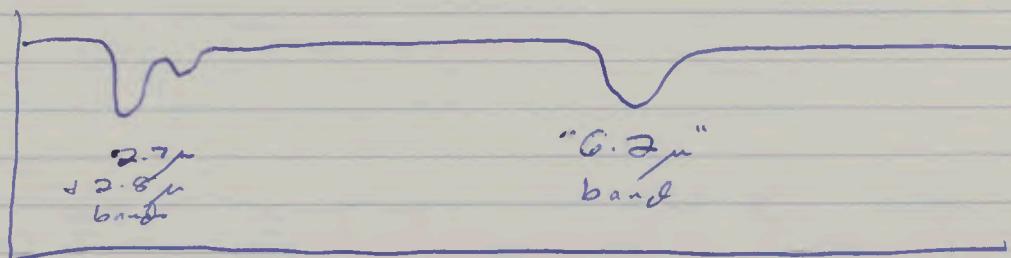
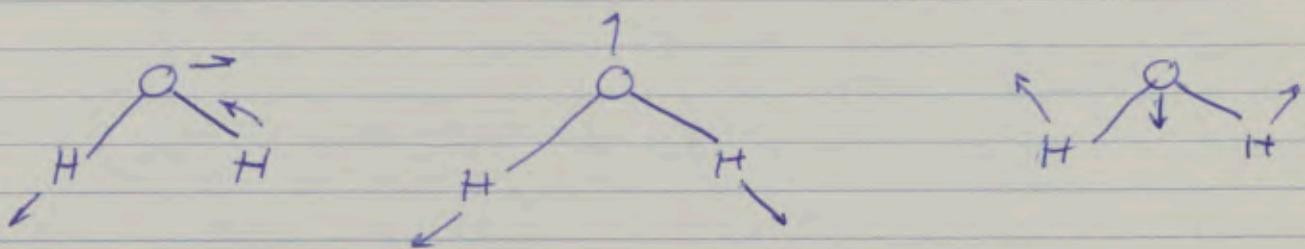
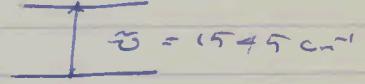
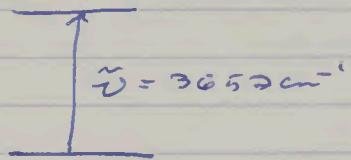
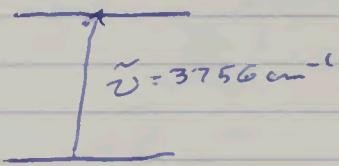
For very loose bonds, each atom has 3 degrees of freedom, so  $3n$  such coordinates for  $n$  atoms. Each represents a degree of freedom, + any position or motion can be described in terms of them. As bond strength increases, degrees of freedom decline, if we demand description of the mol itself. If mol has 3 coordinates for translation + 3 for rotation, degrees of freedom left for the atoms are

$$3n - 6.$$

Note this is simply a reclassification. It gives no vibrational modes. If mol is linear, rot. can occur only about the 2 axes  $\perp$  the molecular axis.  $\therefore$  linear mol. have

$$3n - 5$$

degrees of freedom.  $\therefore$  H<sub>2</sub>O has  $9 - 6 = 3$  and CO<sub>2</sub> has  $9 - 5 = 4$ . For H<sub>2</sub>O,  $\therefore$  3 vibrational energy level patterns (+ overtones).



Actually, high res. vib. spectra show fine structure due to rot. Vib.-rot. spectra in liquid phase  $\exists$  no well-defined rot. energy levels, + rot. fine structure  $\rightarrow$  not observed.  
Hence

$\Delta \nu = \pm 1$  is vib. sel. rule for vib.-rot. spectra.

$\Delta J = \pm 1$  " rot. " "

+ even both  $\pm 1 + -$ , we imp't. in absorption.

Exceptions are provided by molecules w/ an odd electron, like NO. The electron contributes angular mom. about the molecule axis. This permits  $\Delta J = \pm 1$  transitions to occur.

Simplest, & fairly satisfactory approach is to treat mol. as a rigid-rotor, harmonic oscillator system. Then,

$$\tilde{E}_{v,J} = (v + \frac{1}{2}) \frac{1}{2\pi c} \sqrt{\frac{k'}{\mu}} + \frac{\hbar}{8\pi^2 I c} J(J+1)$$

$$\tilde{\omega} = (v + \frac{1}{2}) \tilde{\omega} + \tilde{B} J(J+1),$$

$$\text{where } \tilde{\omega} = \frac{1}{2\pi c} \sqrt{\frac{k'}{\mu}}$$

The transition is  $v=0 \rightarrow v=1$ .

For  $\Delta J = +1$ ; i.e.,  $J \rightarrow J+1$ ,

$$\begin{aligned}\tilde{\nu} &= \frac{3}{2} \tilde{\omega} + \tilde{B} (J+1)(J+2) - \frac{1}{2} \tilde{\omega} + \tilde{B} J(J+1) \\ &= \tilde{\omega} + 2\tilde{B}(J+1), \quad J=0,1,2.\end{aligned}$$

To  $\Delta J = -1$ ; i.e.,  $J \rightarrow J-1$ ,

$$\begin{aligned}\tilde{\nu} &= \frac{3}{2} \tilde{\omega} + \tilde{B} (J-1)J - \frac{1}{2} \tilde{\omega} - \tilde{B} J(J+1) \\ &= \tilde{\omega} - 2\tilde{B} J\end{aligned}$$

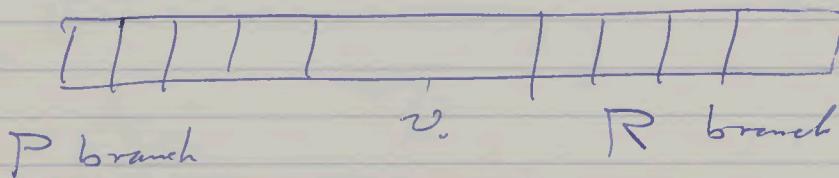
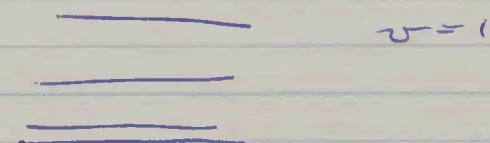
In these expressions, the value of  $J$  is not given. lower state.

- 7 sets of absorption lines spaced in energy by  $2\tilde{B}$ . There is a gap at the band center, corresponding to the absent  $SJ=0$  transition, all of which would have had frequency  $\tilde{\omega}$ .

The low-frequency set is the P branch  
"high" " " " " R "

When  $SJ=0$  is allowed, it is the Q "branch"

The  $2\tilde{B}$  spacing gives I.



Kaylon: line spacing  $\Rightarrow$  on  $2\tilde{B} \Rightarrow$  on I  $\Rightarrow$  hydrogenated mols.

For vib-rot spectrum have 3 Boltzmann eqns  
for the P and R branches:

P branch:

$$N_J = J N_0 e^{-BJ(J+1)/kT}$$

R branch:

$$N_J = (J+1) N_0 e^{-BJ(J+1)/kT}$$

$\therefore$  sum of the two  $\Rightarrow (2J+1) N_0 e^{-BJ(J+1)/kT}$ , correct statistical weights.

What  $J$  is most populated at a given  $T$ ?

P branch

$$\frac{\partial N_J}{\partial J} = 0 = N_0 e^{-BJ(J+1)/kT}$$

$$+ J N_0 e^{-BJ(J+1)/kT} \left[ -\frac{B}{kT} (2J+1) \right]$$

$$\therefore 1 = \frac{B}{kT} (2J^2 + J)$$

$$\therefore \frac{2B}{kT} J^2 + \frac{B}{kT} J - 1 = 0$$

$$J_{\max} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= -\frac{B}{kT} \pm \sqrt{\frac{B^2}{k^2 T^2} + \frac{8B}{kT}}$$

$$= \frac{-B}{kT} \pm \frac{\sqrt{B^2 + 8kT^2}}{kT}$$

- sign gives neg-  $J_{\max}$ , unphysical.

$$\therefore J_{\max} = -\frac{1}{2} + \frac{kT}{2B} \sqrt{\frac{B^2}{k^2 T^2} + \frac{8B}{kT}}$$

$$= -\frac{1}{2} + \frac{1}{2} \sqrt{1 + \frac{kT}{2B}}$$

$\frac{B}{k} \sim 0.3$  in cgs units.  $\therefore \frac{kT}{2B} \gg 1$  at ordinary temp.

$$\therefore J_{\max} \approx -\frac{1}{2} + \frac{1}{2} \sqrt{\frac{kT}{2B}}$$

$$\text{For } T \approx 300^\circ K, \quad J_{\max} \approx -\frac{1}{2} + \frac{1}{2} \sqrt{\frac{300}{0.3}}$$

$$= -\frac{1}{2} + \frac{1}{2} \sqrt{4.9 \times 10^2} = -\frac{1}{2} + \frac{1}{2} (22)$$

$$= 5.3 \approx 5.$$

~~R branch~~

$$\frac{\partial N_J}{\partial J} = 0 = N_0 e^{-B J(J+1)/kT} + (J+1) N_0 e^{-B J(J+1)/kT} \left[ -\frac{B}{kT} e^{2J+1} \right]$$

$$\therefore 1 = \frac{B}{kT} (2J^2 + 3J + 1)$$

$$\therefore \frac{\partial B}{kT} J^2 + \frac{3B}{kT} J + \left( \frac{B}{kT} - 1 \right) = 0.$$

$$\therefore J_{\max} = \frac{-\frac{3B}{kT} \pm \sqrt{\frac{9B^2}{k^2 T^2} - \frac{8B}{kT} \left( \frac{B}{kT} - 1 \right)}}{\frac{4B}{kT}}$$
$$= -\frac{3}{4} \pm \sqrt{\frac{9}{16} - \frac{1}{2} + \frac{1}{2} \frac{kT}{B}}$$

$$\frac{k^2 T^2}{16 B^2} \left( \frac{3B}{kT} \right)$$
$$= \frac{1}{2} \frac{kT}{B}$$

$$= -\frac{3}{4} + \sqrt{\frac{1}{16} + \frac{1}{2} \frac{kT}{B}}$$

$$\approx -\frac{3}{4} + \sqrt{\frac{1}{2} \frac{kT}{B}}$$

$$\text{For } T \approx 300 \text{ K, } \frac{B}{k} \approx 0.3,$$

$$J_{\max} \approx -\frac{3}{4} + \sqrt{4 \cdot 0.3 \times 10^{-2}} = 22 - \frac{3}{4} \approx 21,$$

For vib-rot spectra we again have

$$N_J = (2J+1) N_0 e^{-BJ(J+1)/kT}$$

$$\rightarrow \frac{dN_J}{dJ} = 0 \text{ for PNC}$$

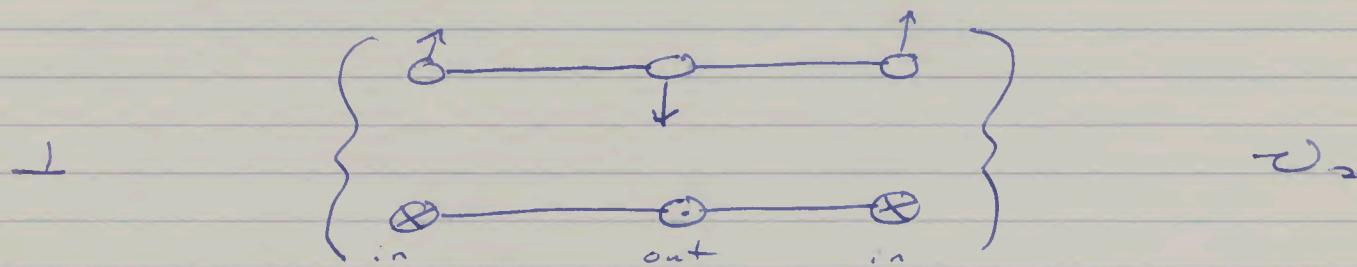
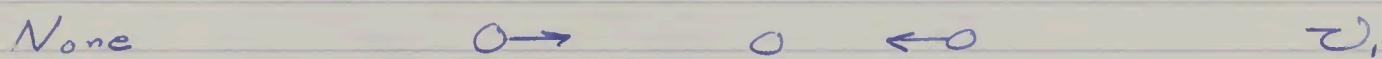
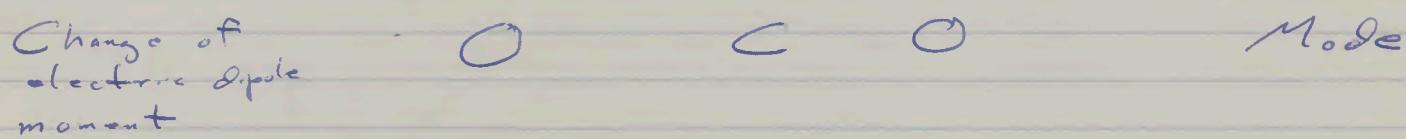
Actually spacing between lines not const. due to coupling between rot + vib.

If one had available a spectrometer of no resolving power, one could determine experimentally, for a specified amount,  $w$ , of absorbing substance, the fraction absorbed  $A_v$ , of the incident radiation at any frequency. In practice, because of the finite width of the slit, one integrates over frequencies. The observed  $A_v$  depends on the slit width  $\Delta v$  and is smoothed over the  $\Delta v$  passed by the spectrometer. But the fractional absorption,  $A$ , over the entire absorption band is const.

$$\int_{v_1}^{v_2} A_v \Delta v = K,$$

provided  $v_1 + v_2$  is taken far enough apart so that in negligible absorption outside these limits.

We have already mentioned that  $3n - 5 = 4$  modes of vibration are expected for  $\text{CO}_2$ . These fundamental frequencies are usually represented as



The  $v_2$  vibration is really the degenerate sum of 2 freqs. In  $v_1$ , the C atom is stationary + the dipole moment is 0 and unchanged. In no pair and class  $v_1$ , vib - rot. lines except in comb. in 3 fundamentals for  $\text{CO}_2$ ,

$$v_2 \quad 667 \text{ cm}^{-1} \quad 15 \mu$$

$$v_3 \quad 2349 \text{ cm}^{-1} \quad 4.3 \mu$$

The bending ( $\perp$ ) vib. takes less energy than the II vib. This "inertial"  $v_1$  can be studied by Raman spectra, + observed frequency  $\sim$

$$v_1 \quad 1388 \text{ cm}^{-1} \quad 7.2 \mu$$

$$\begin{array}{r} 2345 \\ \overline{11745} \\ 1388 \\ \hline 13133 \end{array}$$

This is close enough to  $2\omega_2$  that for a resonance interaction, the Fermi resonance between  $\omega_1$  and  $2\omega_2$  both are displaced from their normal frequencies in comb. bands. Neglecting comb. bands, the vib. energy of  $\text{O}_2$  can be written as

$$E = h(\omega_1 + \frac{1}{2})\omega_1 + h(\omega_2 + \frac{1}{2})\omega_2 + h(\omega_3 + \frac{1}{2})\omega_3.$$

For also. of const. rot. energies. The energy of a transition can then be computed from the diff. between energy levels. The state is written

$$\omega_1 \quad \omega_2 \quad \omega_3$$

where  $l$  is a coupling quantum no. which measures, in units of  $\frac{\pi}{h}$ , the ang. mom. of the C atom about the internuclear axis.

E.g. bands at  $7820 \text{ \AA}$  on  $\text{F}$  are from

$$0 \quad 0^\circ \quad 0 \quad \text{to} \quad 1 \quad 0^\circ \quad 5.$$

Very roughly,

$$\begin{aligned} \Delta E &= \frac{3}{2} h \omega_1 - \omega_1 + \frac{1}{2} h \omega_2 + \frac{11}{2} h \omega_3 - \frac{1}{2} h \omega_1 - \frac{1}{2} h \omega_2 \\ &\quad - \frac{1}{2} h \omega_3 \\ &= h \omega_1 + 5 h \omega_3 \end{aligned}$$

$$\tilde{\omega} = 1388 + 5 \cdot 2349 = 1388 + 11745 = 13133.$$

Observed  $\tilde{\omega} = 12775$ . Comb. terms account for the small diff.

$$y = k_v x = \frac{S}{\pi} \frac{\gamma}{(v - v_0)^2} x; y^{3/2} = \frac{S^{3/2}}{\pi^{3/2}} \frac{\gamma^{3/2}}{(v - v_0)^3} x^{3/2}$$

$$\partial y = x \partial k_v = x \frac{S}{\pi} \gamma \partial (v - v_0)^{-2} = -2x \frac{S}{\pi} \gamma (v - v_0)^{-3} \partial v \\ = -2y^{3/2}$$

$$\int_{-\infty}^{+\infty} (1 - e^{-y}) dy$$

For a strong line, the center of the line is completely absorbed, + any further absorption takes place in the wings only.

$$\therefore k_v = \frac{S}{\pi} \frac{\delta}{(v - v_0)^2}$$

Let  $\alpha = u = k_v g x$ .

$$\therefore \int_{-\infty}^{+\infty} A_v dv = \sqrt{2\pi} \times \int_0^{\infty} (1 - e^{-u}) u^{-3/2} du$$

$$\propto \sqrt{w}$$

$$\therefore A = \sqrt{8\pi \delta^2 \alpha} \quad \text{Not Satisfied}$$

Thus weak lines show linear curves of growth, & strong lines show square-root absorption.

Now a band is composed of a superposition of such rot. lines. For by pressure - paths, the bands overlap & cannot be represented as simple by the same law that the component lines are.

For a pressure, start writing about Doublet bands = together set of curves of growth.

Weak line + strong line bands. If get both, get P + w. o.

$$\int_0^{\infty} u^{-3/2} du = \left[ -\frac{u^{-1/2}}{1/2} \right]_0^{\infty} \quad \therefore A = \sqrt{2\pi} \times 2 \sqrt{k_{v2}} \times$$

$$= \sqrt{2\pi} \times 2 \times \frac{1}{\sqrt{\frac{S}{\pi \delta^2} \times x}}$$

$$= \sqrt{4}$$

Spiral & Adams - Double plates at 7820 Å.  
Measured again widths:

$$A = \int_{v_1}^{v_2} A_v dv = \int_{\lambda_1}^{\lambda_2} A_{\lambda} d\lambda = \bar{A}_{\lambda} \Delta \lambda$$

When  $\bar{A}_{\lambda}$  is set = 1, we have  $\Delta \lambda \stackrel{= w(J)}{=} w(J)$ .  
E.g.,

Plate	Phase	4	6	8	14	18	20	22	24	26	30	34	
		w(J) in mA											
1745	65°	36	42	51	52	51	48	43	48	49	22	31	
3028	67°	32	44	49	73	83	76	56	82	77	70	59	

Even J's because of a nuclear spin selection rule.

Missing J's because of telluric overlapping.

Now 7820 Å is a <sup>band of</sup> weak lines → for a standard clear through,  
 $w(J) \propto g \chi(J) \propto N(J)$ .

$$\frac{N_J}{g(J+1)} = N_0 e^{-B(J(J+1)/kT_{rot})}$$

$$\therefore \log_{10} \frac{w(J)}{(J+1)} = \text{const.} - 0.244 \frac{J(J+1)}{T_{rot}}$$

putting in appropriate value of B.

$\delta$  is the half-width at half-maximum  $k_v$ ,  
or, simply, the half-width of the line.

$$\gamma = \gamma_0 \left( \frac{P}{P_0} \right) \left( \frac{T_0}{T} \right)^{1/2}$$

Comparing lab. w. planetary  
 $\delta$ 's gives P<sub>g</sub>, V<sub>g</sub>, T  
dependences.

where 0 refers to some ref. level. When  $v=v_0$ ,  
 $k_v$  is max., +  $k_v = S/\pi\delta$ . When  $v-v_0 = \pm\delta$ ,

$$k_v = S/2\pi\delta,$$

or  $\frac{1}{2}$  the max. value.

Assume that  $I_0$  is const. within the line's  $\Delta v$ .

$$\therefore A_v = \frac{I_0 - I_v}{I_0} = 1 - \frac{I_v}{I_0} = 1 - e^{-k_v S x}.$$

$$\therefore A = \int_{v_1}^{v_2} A_v dv = \int_{v_1}^{v_2} (1 - e^{-k_v S x}) dv.$$

In the case of a weak line,

$$1 - e^{-k_v S x} \approx k_v S x,$$

and

$$A = S p x \propto P_w$$

The total absorption is  $\propto$  to the amount of gas.

Absorption by a single spectral line:

In the lower atm & troposphere, the shape of a spectral line is essentially determined by pressure broadening alone. Doppler, Stark, + Zeeman effects are generally ~~neglected~~ <sup>not taken into account</sup>.

Consider end of intensity  $I_v^0$  incident upon a slab of thickness  $x$ . Some of radiation will be absorbed, and some transmitted. At any pt. within the slab, the loss of energy  $\propto I_v^0$  and to g.  $\therefore$  in each thickness  $dx$ ,

$$dI_v = -k_v I_v g dx$$

where  $k_v$  is a mass absorpt. coeff. characteristic of the material.

$$\therefore I_v = I_v^0 e^{-k_v g x} = I_v^0 e^{-\tau}$$

The relation is true only for monochromatic radiation, since  $k_v$  is func. of  $\nu$ . For a pressure-broadened absorption line, the variation of  $k_v \sim \nu$  is given by the Lorentz line-shape:

$$k_v = \frac{S}{\pi} \frac{\delta}{(\nu - \nu_0)^2 + \delta^2}$$

in eq. derived from consid. of broadening of energy levels by the field of impinging atoms.  
S is called the integrated absorption coeff., i.e.

$$\int_{-\infty}^{+\infty} k_v d\nu = S$$

The between cells  
dist. determines line shape.

Sagan & Pollack (1971) JGR 72 469

Anisotropic nonconservative scattering ...

$$\frac{1}{\sqrt{3}} \frac{dI_+}{d\tau} = -I_+ + I_+ \tilde{\omega}_0(1-\beta) + I_- \beta \tilde{\omega}_0$$

$$-\frac{1}{\sqrt{3}} \frac{dI_-}{d\tau} = -I_- + I_- \tilde{\omega}_0(1-\beta) + I_+ \beta \tilde{\omega}_0$$

↑  
two stream  
average of  $\mu$

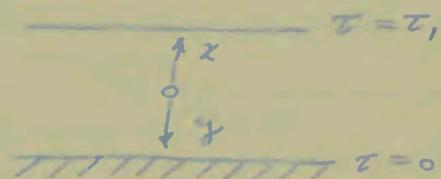
forward & back scatter

$$\frac{dx}{d\tau} = ax + by \quad x = I_+ \quad a = \sqrt{3} [\tilde{\omega}_0(1-\beta) - 1]$$

$$-\frac{dy}{d\tau} = ay - bx \quad y = I_- \quad b = \sqrt{3} \beta \tilde{\omega}_0$$

$$(D-a)x = by$$

$$-bx = (D+a)y$$



$$(D+a)(D-a)x = (D+a)by$$

$$(D^2 - a^2)x = -bx^2$$

$$[D^2 - (a^2 - b^2)]x = 0 \quad (D^2 - c^2)x = 0 \quad \frac{d^2x}{d\tau^2} = c^2x$$

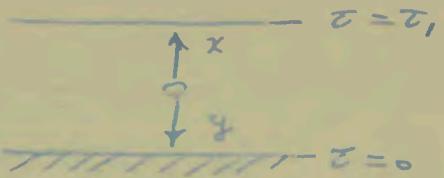
$$c^2 = a^2 - b^2 = 3 \left[ (\underbrace{1 - \tilde{\omega}_0}_{1-\beta}) (\underbrace{1 - \tilde{\omega}_0}_{\beta}) + 2 \beta \tilde{\omega}_0 \right] = 3u^2(1 - \tilde{\omega}_0)^2$$

where  $u^2 = 1 + \frac{2\beta\tilde{\omega}_0}{1 - \tilde{\omega}_0}$

$$x = fe^{c\tau} + ge^{-c\tau}$$

$$y = \frac{1}{b}(D-a)x = \frac{c-a}{b}fe^{c\tau} - \frac{c+a}{b}ge^{-c\tau}$$

$$x = fe^{c\tau} + ge^{-c\tau}$$



$$x_0 = 0 \quad f + g = 0 \quad g = -f$$

$$x = f(e^{c\tau} - e^{-c\tau})$$

$$y = \frac{c-a}{b} fe^{c\tau} - \frac{c+a}{b} ge^{-c\tau}$$

Can show  $\frac{c-a}{b} = \frac{u+1}{u-1}$        $\frac{c+a}{b} = -\frac{u-1}{u+1}$

$$\begin{aligned} y &= \frac{u+1}{u-1} fe^{c\tau} - \frac{u-1}{u+1} fe^{-c\tau} \\ &= f \left[ \frac{(u+1)^2 e^{c\tau} - (u-1)^2 e^{-c\tau}}{u^2 - 1} \right] \end{aligned}$$

$$\begin{aligned} R &= \frac{x_0}{y_0} = \frac{(e^{c\tau_1} - e^{-c\tau_1})(u^2 - 1)}{(u+1)^2 e^{c\tau_1} - (u-1)^2 e^{-c\tau_1}} \\ &= \frac{(u+1)(u-1)(e^{\tau_{\text{eff}}} - e^{-\tau_{\text{eff}}})}{(u+1)^2 e^{\tau_{\text{eff}}} - (u-1)^2 e^{-\tau_{\text{eff}}}} \end{aligned}$$

$$\begin{aligned} T &= \frac{y_0}{x_0} = \frac{(u+1)^2 - (u-1)^2}{(u+1)^2 e^{c\tau_1} - (u-1)^2 e^{-c\tau_1}} \\ &= \frac{4u}{(u+1)^2 e^{\tau_{\text{eff}}} - (u-1)^2 e^{-\tau_{\text{eff}}}} \end{aligned}$$

where  $\tau_{\text{eff}} = c\tau_1$

$$x = fe^{ct} + ge^{-ct} \quad y = \frac{u+1}{u-1} fe^{ct} + \frac{u-1}{u+1} ge^{-ct}$$

$$x_0 = Ay_0 \quad f+g = A\left(\frac{u+1}{u-1}f + \frac{u-1}{u+1}g\right)$$

$$g = -Bf \quad B = \frac{1-A \frac{u+1}{u-1}}{1-A \frac{u-1}{u+1}}$$

$$x = f(e^{ct} - Be^{-ct}) \quad y = f\left(\frac{u+1}{u-1}e^{ct} - \frac{u-1}{u+1}Be^{-ct}\right)$$

$$\begin{aligned} R &= \frac{x_{\tau_1}}{y_{\tau_1}} = \frac{(e^{c\tau_1} - Be^{-c\tau_1})(u^2 - 1)}{(u+1)^2 e^{c\tau_1} - (u-1)^2 Be^{-c\tau_1}} \\ &= \frac{(u+1)(u-1)(e^{c\tau_1} - Be^{-c\tau_1})}{(u+1)^2 e^{c\tau_1} - (u-1)^2 Be^{-c\tau_1}} \end{aligned}$$

$$\begin{aligned} J &= \frac{y_0}{y_{\tau_1}} = \frac{(u+1)^2 - (u-1)^2 B}{(u+1)^2 e^{c\tau_1} - (u-1)^2 Be^{-c\tau_1}} \\ &= \frac{(u^2 + 1)(1 - B) + 2u(1 + B)}{(u+1)^2 e^{c\tau_1} - (u-1)^2 Be^{-c\tau_1}} \end{aligned}$$

Conservative scattering  $\omega_0 \rightarrow 1$

$$\tau_{\text{eff}} = 3^{1/2} u/(1-\omega_0)\tau_1 = \sqrt{3(1-\omega_0 + 2\beta\omega_0)(1-\omega_0)}\tau_1$$

$$\approx \sqrt{3(2\beta)(1-\omega_0)}\tau_1 \rightarrow 0$$

so can write  $e^{\pm\tau_{\text{eff}}} \approx 1 \pm \tau_{\text{eff}}$ . Then

$$J = \frac{4u}{(u+1)^2 e^{\tau_{\text{eff}}} - (u-1)^2 e^{-\tau_{\text{eff}}}} \approx \frac{4u}{(u+1)^2 (1+\tau_{\text{eff}}) - (u-1)^2 (1-\tau_{\text{eff}})}$$

$$= \frac{4u}{[(u+1)^2 - (u-1)^2] + \tau_{\text{eff}} [(u+1)^2 + (u-1)^2]}$$

$$= \frac{4u}{4u + 2\tau_{\text{eff}}(u^2 + 1)} = \frac{4u}{4u + 2\sqrt{3}u(1-\omega_0)\tau_1(u^2 + 1)}$$

$$= \frac{1}{1 + \frac{\sqrt{3}}{2}(1-\omega_0)\tau_1(u^2 + 1)}$$

Now  $u^2 = 1 + \frac{2\beta\omega_0}{1-\omega_0}$ , so  $u^2 + 1 = 2\left(\frac{1-\omega_0 + \beta\omega_0}{1-\omega_0}\right)$ .  
thus

$$J \approx \frac{1}{1 + \sqrt{3}\tau_1(1-\omega_0 + \beta\omega_0)} \approx \frac{1}{1 + \sqrt{3}\beta\tau_1}$$

$$\approx \frac{1.16}{2\beta\tau_1 + 1.16}$$

Nonconservative isotropic scattering with  $\tau_1 = \infty$

$$\left. \begin{array}{l} \omega_0 \neq 1 \\ \rho = \frac{1}{2} \\ \tau_1 = \infty \end{array} \right\} \quad u^2 = \frac{1 - \omega_0 + 2\rho\omega_0}{1 - \omega_0} = \frac{1}{1 - \omega_0}$$

$$\tau_{\text{eff}} = 3^{1/2} u (1 - \omega_0) \tau_1 = 3^{1/2} (1 - \omega_0)^{1/2} \tau_1 = \infty$$

$$\begin{aligned} R &= \frac{(u+1)(u-1)(e^{\tau_{\text{eff}}} - e^{-\tau_{\text{eff}}})}{(u+1)^2 e^{\tau_{\text{eff}}} - (u-1)^2 e^{-\tau_{\text{eff}}}} = \frac{u-1}{u+1} \\ &= \frac{1-1/u}{1+1/u} = \frac{1 - \sqrt{1-\omega_0}}{1 + \sqrt{1-\omega_0}} \end{aligned}$$

$$J = \frac{4u}{(u+1)^2 e^{\tau_{\text{eff}}} - (u-1)^2 e^{-\tau_{\text{eff}}}} = \frac{4u}{(u+1)^2 e^{\tau_{\text{eff}}}} = 0$$

$$\alpha = 1 - R - J = 1 - R$$

$$\omega_0 = 0.1 \quad R = \frac{1 - \sqrt{0.9}}{1 + \sqrt{0.9}} = \frac{0.051}{1.949} = 0.026$$

$$\omega_0 = 0.5 \quad R = \frac{1 - \sqrt{0.5}}{1 + \sqrt{0.5}} = \frac{0.293}{1.707} = 0.172$$

$$\omega_0 = 0.9 \quad R = \frac{1 - \sqrt{0.1}}{1 + \sqrt{0.1}} = \frac{0.684}{1.316} = 0.520$$

$$\omega_0 = 0.975 \quad R = \frac{1 - \sqrt{0.025}}{1 + \sqrt{0.025}} = \frac{0.842}{1.158} = 0.727$$

$$p = \omega_0(1 + \cos \theta) ; \quad \tau_i = \infty$$

$$\begin{aligned} 2\beta &= 1 - \int p \cos \theta \frac{d\Omega'}{4\pi} = 1 - \omega_0 \int (1 + \cos \theta) \cos \theta \sin \theta d\theta \frac{d\Omega'}{4\pi} \\ &= 1 - \frac{\omega_0}{2} \int_0^\pi (1 + \cos \theta) \cos \theta \sin \theta d\theta \\ &= 1 - \frac{\omega_0}{2} \int_0^\pi \cos^2 \theta \sin \theta d\theta = 1 - \frac{\omega_0}{3} \end{aligned}$$

$$\begin{aligned} u &= \frac{1 - \omega_0 + 2\beta\omega_0}{1 - \omega_0} = \frac{1 - \omega_0 + (1 - \frac{\omega_0}{3})\omega_0}{1 - \omega_0} \\ &= \frac{1 - \frac{1}{3}\omega_0^2}{1 - \omega_0} \end{aligned}$$

$$\text{With } \tau_i = \infty, \quad R = \frac{u-1}{u+1}, \quad T = 0, \quad Q = 1 - R$$

$\omega_0$	$R$
0.1	0.025
0.5	0.150
0.9	0.460
0.975	0.680

For  $\omega_0 = 1$  and  $\tau_1 = 20$

$$T = \frac{1.16}{2\beta\tau_1 + 1.16} \quad 2\beta \approx 1 - \frac{1}{3}\omega_1$$

$$\therefore T \approx \frac{1.16}{(1 - \frac{1}{3}\omega_1)\tau_1 + 1.16} = \frac{1.16}{20(1 - \frac{1}{3}\omega_1) + 1.16}$$

Agrees with the table for various  $\omega_1$ .

$\beta, \omega_0 \rightarrow \infty$ . Trade assumptions for many scatterings. Effect of surface



## Critical Review

- A. Intro.
- B. Origin of Life. +
- C. Environmental specifications:  $\text{H}_2\text{O}$ ,  $\text{C}$ ,  $\text{O}_2$ , +
- D. Direct evidence
  - a. Chondrites
  - b.  $\text{O}_2$  isotope seasonal changes; no correlation.
- E. Intelligence

### A. Introduction

Ladies & gentlemen, it is my pleasant duty <sup>task</sup> to sever discuss with you some aspects of extraterrestrial life, that never-never land between astronomy and biology. <sup>on the one hand</sup> ~~on the other~~ <sup>on the one hand</sup> borders we now stand find ourselves standing. Dr. Russell has given an excellent summary of the pertinent physical & chemical information, & evolutionary hypotheses, which we have about the planets, and I will rely on his presentation. There are three general approaches to the problem of extraterrestrial life. First, we can ask how general were the processes leading to the origin of life on earth. Second, ~~and if they are very general~~, we second we may investigate the planetary environments, and inquire what the likelihood is that similar lifeforms can there survive and grow. Thirdly, we may ~~search for~~ look for direct evidence for extraterrestrial life. I would like to discuss these approaches in this sequence. I will try to separate fact from speculation, and distinguish the enthusiasts from the pessimists. Almost every issue of consequence, it turns out, has two sides.

## B. Origin of Life

To talk of life, we must have some idea of true life, the one that we, overall, wish we are common ~~and~~ is inhabitant.

1. Contemporary terrestrial organisms all have a common biochemical ground plan.

DNA, RNA, messenger<sup>+</sup>, adapted protein, enzymes.  
DNA synthesis from triphosphates, ATP + ADP.

2. These common substances, are they rare mols. selected for their efficiency, or are they easily produced?

Miller - prim. amino, hydroxyls ==  
amino + hydroxy acids. Corroborating  
uv. Intermediate steps involve cyanides  
+ aldehydes.

Adeins produced by electron beam irradiation  
of CH<sub>4</sub>, NH<sub>3</sub>, H<sub>2</sub>O + H<sub>2</sub> + by uv irradiation  
of dilute sol. HCN. Dr. Damm also  
found in little spots: Oro, Ponmampum,  
+ co-workers.

UV irrad. of dilute aldehyde sols  
produce ribos → 2-deoxyribose.  
Balance of sugar alcohols.

Some expectation of phosphates in prim. seas.  
all building blocks of nucleic acids need  
P-P + Sigma makes nucleoside triphosphates,  
e.g., ATP. We have not yet done  
w. 2-deoxyribose. If that succeeds we are  
up to Kornberg or anyone replaced by  
time. i.e. from prim. atmos. to self-  
replicating polynucleotide understood,  
& it is sometimes said, not selu.  
then takes over, & we understand it.  
Subsequent evol. to present initial cond. Butler's  
aphorism: This may be an important  
part of the story, but not all of it.

### 3. Criticisms

- a. All these mols may be used later because they are efficient. Earliest life-forms may have been very diff. Price
- b. Pure soils instead of grunk. Miller Monte de  
Miller
- c. Ethyl metaphosphate not most common P compd. in prim. environ.
- d. No environmental control Elaborate ~~contemporary~~ opportunities. Rich + Stent.

Much still to be performed on origin of life. But results so far - only 10 yrs. since Miller's classic exp't - are extremely encouraging & give us some confidence that proteins + nucleic acids may be dominant elsewhere, & that life arises easily. Morphology elsewhere, diff., of course. This makes life-detection exp'ts easier, but it also makes the risk of biology. contam. much higher. [Insert from Denver p. 7]

#### 4. Panspermia

#### C.B. Environments

There are locales in our solar system where the events leading to origin of life may today be occurring. 4. Depending on  $\text{NH}_3$  abundance, Dallet has a  $\text{H}_2\text{O}$  cloud larger at

$$10^{-3} \text{ gm cm}^{-3} \leq \rho \leq 10^3 \text{ gm cm}^{-3}$$

$$\text{and } 200^\circ\text{K} \leq T \leq 400^\circ\text{K}.$$

From afar least prob. for life in solar systems.

xerobiotic?

♀, ♀, ♂ : subsurface -  $\frac{1}{3}$  H<sub>2</sub>O, org. matter, heat suggestion based  
on various evidence. Direct obs needed

♂ : Cond. no doubt severe. Alfred Russel Wallace  
(1907). Expt's performed using known organisms  
& selective culture techniques. Reported live  
symposia. Both survived + growth reported.

Drooth especially difficult to assess  
because of starvation replication w. no oxygen  
mass increase.

H<sub>2</sub>O content of soil similar to the Martin?  
What's the Martin w/?

But most literature in soil science + food  
sci.  $\Rightarrow$  survival + growth. Relevant for  
contam., not for ♂ biology - except  
to suggest that mechanism exists.

#### D. Direct evidence

1. Carbonaceous chondrites like we get from.

a. Org. matter: Berthelot, Bergelin, Wöhler.  
+ few % by mass + not carbon. Somewhere  
a lot of org. matter was made. Asteroid?  
♂?

b. Organized elements. Clays + Niggs. Andrus, Fish

c. Visible organic. Soder + Newton.  
Facultative anaerobe.

2.  $\sigma$

2 L.Fa on  $\sigma$ .

→ a. Green

→ b. Canals

c. Wave of darkening + color  $\Delta S$  - <sup>-Organisms</sup> Deliquescent salts

d. Scalar  $S^2$ .

d. Polarimetric evidence - <sup>- growth</sup> size change due to H<sub>2</sub>O adsorption. (Not enough H<sub>2</sub>O, prob.)

e. IR spectrum. If absorption, at 3.45, 3.58, + 3.69  $\mu$ . But refl. complicates. If absorb., only identifier which has been proposed, + which explains the features are HC + CH<sub>3</sub>CHO. On  $\sigma$ , CH<sub>3</sub>CHO will be a gas when  $T \geq 240^\circ\text{K}$ . Thus, you a gas in day, + condense <sup>relatively little even</sup> at night. Two approaches: gas is absurd, so it's something else I don't understand. Other approach is to ask how th gas makes sense. Aldehyde polymerization  $\xrightarrow{\text{uv}}$  organic. Might we here have a kind of a Fischer, utilizing uv? Need glass envelope, opaque in vis., temps. in ir + uv. No H-C's.

If we take optimistic side of all the above, what do we have? We don't even know if the data all refer to the same organism. Still possibl of blind man + elephant, but with many a lot of other big animals added.

If we nevertheless assume a common origin,  
the following picture emerges:

An organism, 0.1 to 1 mm in size, with a  
fleshy cover, transparent in infra-red, + opaque - visible.  
Color predominantly gray, sometimes brown,  
green, blue, etc. Contains  $\text{CH}_3\text{CHO}$  inside envelope.  
Cover a few tens of % of the life areas. Changes  
color, size, + reflectivity in varying when  $\text{H}_2\text{O}^+$   
content greatest.

Of course this description may be ~~totally~~  
wrong. But it does emphasize that if  $\exists$  life on  
 $\sigma$ , it will ~~most~~ likely be very unfamiliar.

No one's going to improve our understanding  
& prove life on  $\sigma$ , without actually landing there.

(1) High topographic resolution.

(2) Second  $\Delta$  is bands.

(3) Correlation blue during w. polarimeter or spectrophotograph  
or vis. obs.

Soon  
~~eventually~~ we will have the capability for  
landing instruments  
~~which~~ for  $\sigma$ . biology exploration. We must prepare  
for that unique opportunity. It will only  
come once. ~~Our scientific descendants~~ Scientists  
of future generations will judge how well we do.

M 31: Other opportunities may exist, but they  
will be inaccessible for a long time.

Microwave cells "conductive" theor. temp. when heating  
 on  $\pi R^2$ , conduction results <sup>heat from jet</sup> ~~in cooling from  $\pi R^2$~~ ,  
 both hemispheres.

If  $\varphi$  microwave limb-darkening cannot be explained by atmos. absorption, then might it not — as is probably the case for the limb-darkening — be explainable by absorption + scattering by a cloud layer. Is there possibly a H-C layer in the lower atmosphere? Plot H-C v p curves vs. atmos. v.p. curves. Likely H-C's from high pressure  $N_2$ ,  $H_2O$ ,  $CO_2$  interaction. Note v.p. curves not isothermal, but absolute.

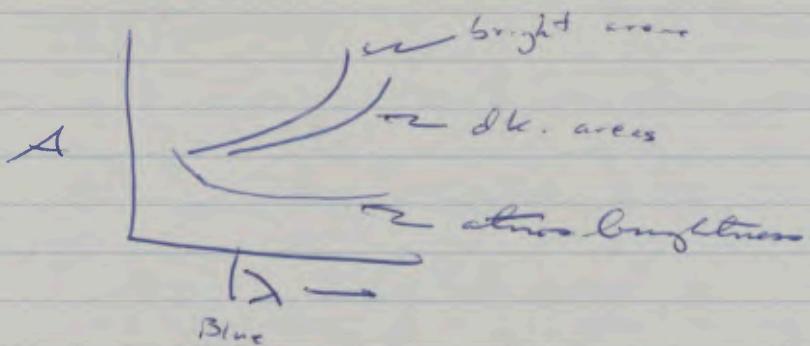
- Dollfus'  $A = A(\lambda)$  permits an integration,

$$A_{bol} = \frac{\int A(\lambda) B_\lambda d\lambda}{\int B_\lambda d\lambda} : B_\lambda \text{ at } T \approx 5650^\circ K.$$

+ will give an  $A_{bol} \approx 0.20$  for both bright + dark areas. Extrapolation beyond  $\lambda \approx 8000 \text{ \AA}$  can be made (1) by assuming  $A_{\lambda > 8000 \text{ \AA}} = A_{\lambda = 8000 \text{ \AA}}$ , or by (2) extension of existing slope. This gives "in" + more values of  $A_{bol}$ .  $\therefore$  computed  $T$  for airless  $\oplus$  will be  $44 - 319^\circ K.$   $\therefore$  greenhouse effect very important. There I suspect that even with  $w_{CO_2} = 100 \text{ m-stw}$  +  $w_{H_2O} = 10^{-2} \text{ g cm}^{-2}$ , greenhouse effect will not be sufficient to explain observed temp w. emissivity correction [Note Res thinks  $T \propto \epsilon^{-1/4}$  for 1 $\mu$  window. Actually less steps.]  $\therefore$  another absorber on  $\oplus$ .  $CH_3CHO$ , e.g.? Scattering by dust?

- Seems to exist a  $\odot$  argument regarding  $CO_2$  +  $P_s$  on  $\oplus$ . To photometer, polarimeter, determine of  $P_s$ , and  $w_{CO_2}$ , basically. Rayleigh coefficient of  $CO_2$ . But to determine  $w_{CO_2}$  and  $P_s$  for the pressure broadening.

Dollfus plots out blue haze may be mostly illusory.



I.e., contrast initially declines towards w.  
Blue haze may simply represent the tendency of blue clouds to form in bright areas, thereby enhancing the contrast initially.  
I see evidence bright areas are higher & are more likely to have clouds above them. Residual frost near pole esp. not more frequently left in bright areas than in dark. Also Dollfus detected polarimetrically one effect deposit on Nix Olympia, which is in a bright area.

# Chromatography Notes

Aniline Hydrogen Phthalate spray  
for Sugars

0.93 gm aniline

1.66 gm phthalic acid - 8.30

100 ml H<sub>2</sub>O saturated w.<sup>N</sup> Brtaam

Relative 164 : 493, 1979

5 min at 105 °C Develops.

## Chromatography Systems

### Amino acids

Lut. dme: Ethanol: Water

55: 25: 20

$\alpha$ -Propanol - Ammonia - Water

40 : 30 : 10

Acetone : 25% Trichloroacetic Acid

75 : 25

25 gm Trichloroacetic Acid + enough H<sub>2</sub>O  
to make 100 cc.

100 gm to 400 cc.

Beaker weighs 112.5 gm.

add 50 gm solid trichloroacetic acid  
so total weighs 162.5 gm.

Add 200 cc. water

n-Propanol: Ethyl acetate: Water

7: 1: 2

To make 1500 ml,

$$\text{n Propanol: } 700 + 350 = 1050$$

$$\text{Ethyl acetate: } 100 + 50 = 150$$

$$\text{Water: } 200 + 100 = \frac{300}{1500 \text{ ml}} \checkmark$$

(Actually mixed 500 ml total)

n Butanol: Acetic acid: water

4: 1: 5

To make 1500 ml,

$$\text{n Butanol: } 400 + 200 = 600$$

$$\text{Acetic acid: } 100 + 50 = 150$$

$$\text{Water: } 500 + 250 = \frac{750}{1500 \text{ ml}} \checkmark$$

$\lambda = 1 \mu\text{liter}$

①

Whatman #4 washed w. <sup>1% solution</sup> Oxalic acid + folded  
Rinsed w. distilled H<sub>2</sub>O  
Dry overnight

Whatman #1 is a slow paper.

Sample evacuate until bubbling stops.

Freeze in N<sub>2</sub>↓ dewar

Evacuate to ~150  $\mu\text{pp}$  air.

Then, if required, add H<sub>2</sub>.

### Intermediate

Then access of air is given to the samples.

Add unlabeled carrier.

Mark paper for origin.

Turn hairdryer to hot & on.

For simultaneous spotting of several papers,

back origins w. glass to insure reabsorption  
& prevent spotting of underlying papers.

(2)

Spot 1 drop on origin w. disp. pipette.

Blow Dry w. hair dryer.

Add and drop. Dry.

Continue until sol. depletion. > 10.

(Do not touch glass <sup>pipette</sup> to paper)

If too much sample + carrier, first  
evaporate w. evaporator. Be careful to wash  
all parts of evaporator which will have contact w. sol.

Label papers below origins, at lower rt. corner.

Do not heat u. dryer longer than necessary.

↑ some poss. of thermal degradation of sample.

(3)

Wash + rays.

Put paper on tray; hold w. weight.

Put first solvent system at bottom of chromatography cabinet, below, but not touching paper.

Seal cabinet, + let solvent permeate cabinet (at least 30 min.; sometimes overnight).

Drop ~ 100 ml of the same solvent system through funnel into tray.

Let for ~ 5 or 6 hrs for most solvent systems; or enough for spot to move  $\frac{2}{3}$  to  $\frac{3}{4}$  of paper, but not off it. (Not usually for overnight).  
or it moves off the paper altogether

(4)

Then open to exhaust system + open & holes.  
Leave overnight to dry.

Next A.M. remove paper remove dish at bottom.

Cut fold. w/ paper cutter.

Turn so origin moves from upper left to  
upper right. Fold again.

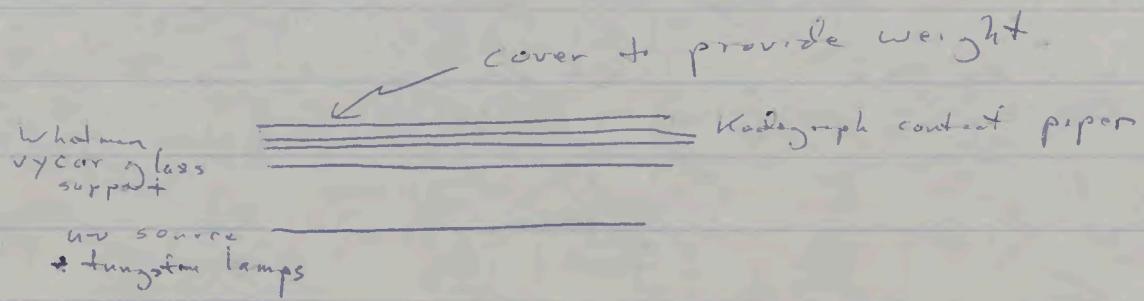
Put new solvent system in bottom of cabinet  
+ repeat everything as before.

Now autoradiography, shadowgrams, + end-window counting

Autoradiography

Shadowgrams:

In dark room.



(5)

Stamp w. radioactive ink.

$\frac{1}{2}$  sec uv dose (uv lamp has timer)

developing sol. until can see developing (red lit. a).  
dilute acetic acid bath <sup>until</sup> rinses (w/ rubber gloves).

>5 min in fixer (hypo).

hypo clearing agent (reduces regenerating time)  
rinses in water for ~ 10 min in special trays.

About  $\frac{1}{2}$  hr in all.

Dry <sup>contact</sup> paper in drying machine.

While developing above, make contact of paper  
with X-ray film.

2 types " " blue-sensitive, & no-screen.

No screen less emulsion on both sides.

Fold white paper around X-ray film.

Put in X-ray folder.

## A CONCINENCE TECHNIQUE FOR PAPER CHROMATOGRAPHY OF SOME BIOLOGICALLY IMPORTANT COMPOUNDS

The almost explosive growth of chromatographic methods during recent years has provided us with powerful tools for the separation of a wide variety of chemical substances. Such diverse materials as complex macromolecules of biological systems or the fission products from atomic piles have been effectively separated by these new methods.

The impetus given to the use of paper chromatography by the Cambridge group of workers under A.J.P. Martin has resulted in the great popularity of this technique. The isolation and identification of trace quantities of a host of natural and synthetic substances has thus been made possible.

The Rf value or ratio of distance traveled by substance to the distance traveled by solvent front, is generally used as the criterion of identity. If two substances have the same Rf values in two or more solvent systems, they are assumed to be identical. But although one often sees in the literature, Rf values quoted to an astonishing degree of precision, experience shows that Rf values are at best only a rough guide, and should not be used as the sole means of identifying a substance.

Rf values are dependent on a large number of variables, among which may be mentioned:

1. Composition of development phase
2. Kind of paper
3. Direction of paper
4. Manner of development (descending, ascending, ascending-descending, radial).

5. Length of paper used for development
6. Distance of starting line from solvent
7. Concentration of solute
8. Presence of other substrates
9. Temperature of development

The uncertainty accompanying the identification by Rf values alone is illustrated very pertinently from the following case study from some of our own work on the radiolysis of adenine. The first slide is an autoradiograph of an irradiated solution of adenine. Two major products are indicated, A and B. We identified A as 4,6-diamino 5-formamido pyrimidine and B as 8-hydroxyadenine. The chromatographic identification was further confirmed by chemical test and ultraviolet spectrophotometry.

However, at the same time another group of workers reported that compound B was Adenine 1-N-oxide, basing their identification on Rf values. The following Rf values for 8-hydroxyadenine and Adenine 1-N-oxide indicated that no differentiation could have been made on this criterion alone:

	ADENINE-8-OH	ADENINE-1-N-OXIDE
Propanol-Ammonia-Water	.47	.51
Butanol-Propionic Acid	.61	.66
Isobutric Acid-Ammonia	.54	.58
Butanol-Water	.62	.64

To establish the identity of compound B the chromatography of the original sample was repeated, adding adenine-1-N-oxide as a carrier. (The

solvent systems were composed of Propanol-Ammonia-Water and Butanol-Propionic Acid-Water.) The next slide demonstrates the results obtained. The bright areas on the shadowgram are the Adenine-1-N-oxide and the residual adenine. The dark spot B on the autoradiograph appears to be coincident with the bright area on the shadowgram.

The experiment was then repeated in two other solvent systems. Isobutyric acid-ammonia and Butanol-Water. The results are shown in the next slide. The spot produced by the unlabeled Adenine-1-N-oxide has shifted further away from the radioactive spot B, as shown in slide #3. If B was indeed Adenine 1-N-oxide, the radioactivity and the absorption would have coincided in both systems as in the case of the residual Adenine.

In our experimental work we have developed a technique which gives unambiguous results. Ultraviolet absorption photography has been used as early as 1949 by Markham and his co-workers for the location of purines and pyrimidines. Autoradiography has been extensively used since the pioneering work of Calvin and his associates with C<sup>14</sup>. In the work we are presenting, the two techniques have been combined as one operation. This method has been successfully used for purines, pyrimidines, amino acids and sugars. C<sup>14</sup> labeled compounds are used as starting materials in all reactions studied. Non-radioactive carriers of the assumed resultant products of the experiment are added to the original material before spotting. The material is co-chromatographed in two dimensions on Whatman No. 4 paper, previously washed with oxalic acid.

Autoradiographs are prepared by placing an x-ray film in close contact with the chromatogram for a period determined by the amount of radioactive material present. This time may range from one day to six months. We have found that 10,000 dpm or five micromicrocuries produces a spot on the x-ray film in approximately a week. Radioactive compounds appear as dark spots on the transparent x-ray film. If the radioactive products are identical with the carriers, the dark spots on the autoradiograph will correspond precisely to the brightenings of the shadowgram.

When working with purines, pyrimidines, and other ultraviolet absorbing products, the shadowgrams are prepared by shining an ultraviolet light through the chromatogram on to Kodagraph contact paper. A G.E. germicidal lamp was used as the uv source from a distance of ten inches. The time of exposure is 1-2 seconds. To insure close contact of the papers and therefore sharper prints, a sheet of vycor glass which transmits light of the wavelength at which purines and pyrimidines absorb is placed between the light and the paper. The ultraviolet absorbing areas on the chromatogram appear as well-defined white spots on a dark background.

The next slide illustrates an experiment confirming the formation of adenine by the electron irradiation of a mixture of  $\text{CH}_4$ ,  $\text{NH}_3$  +  $\text{H}_2\text{O}$ . Radioactive compounds appear as dark spots. The non-radioactive carriers appear as bright spots on a dark background.

For greater certainty, the area corresponding to the matching dark and bright spots is cut out from the paper chromatogram, eluted with a suitable solvent, and rerun in two different solvent systems. This is

the equivalent of analysis in four single systems by any other means. If coincidence is established with this repeated procedure, the positive identification of the material can be assumed.

With amino acids or sugars, the carriers are located on the chromatogram with the aid of a color reaction. The shadowgram is prepared in the same manner as for the purines and pyrimidines, but a visible light source is used instead of an ultraviolet light. The colored areas absorb the light and a well-defined bright spot appears on a dark background. The following three slides demonstrate the results obtained with purines and pyrimidines, with amino acids, and with sugars. In all these cases, it is understood that the amount of radioactive material is insufficient to be detected by a shadowgram alone.

This identification technique can be performed in reverse order also. When starting with unlabeled material, a radioactive carrier is added before spotting. The amount of radioactive product should be below the limit of detectability for the shadowgram but large enough to produce a dark spot on the x-ray film. (The limit of detectability for purines and pyrimidines is about 0.003 ug of material. For amino acids, the limit is .04 ug).

The next slide illustrates this reverse procedure. The identification of a trace amount Guanine which was synthesized during the thermal polymerization of amino acids.

Our work has been primarily concerned with purines, pyrimidines, amino acids and sugars. This coincidence technique, however, can be applied to

many other compounds which will give a color reaction such as fatty acids, peptides, steroids, etc., in fact, to any compound which can absorb ultra-violet or visible light. The application of this coincidence technique provides an unambiguous identification of compounds without the uncertainty involved in using Rf values and often eliminating the need for tedious chemical analysis.

Chromatography  
Protocol and  
Equipment Notes

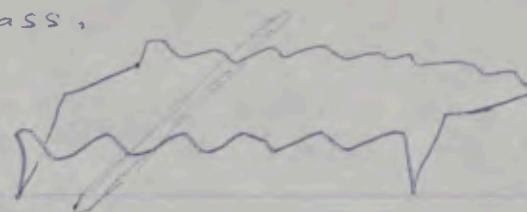
"Spectrometric Ident. & Fication of  
Organic Compounds" — Silverstein  
Bassler, Wiley, 1963

Vycor tubes + glass stopcocks.

New England Nuclear Corp.  
575 Albany Street  
Boston 18, Mass.

Freezer for  
unstable chems.

Pipette long



2.4 ml  $\text{H}_2\text{O}$  to Adams & C'  $\rightarrow 3 \times 10^{-3} \text{ M}$  sol. add  
500  $\mu\text{l}$  of this "sol."

Add  $\sim 25 \mu\text{l}$   $\beta$ -D-Deoxyribos + agn6

For stoichiometric proportion add  $\text{H}_3\text{PO}_4$  45  $\mu\text{l}$ .  
of 0.01 M sol.  $\text{H}_3\text{PO}_4$  + 130  $\mu\text{l}$

500  $\mu\text{l}$

20  $\mu\text{l}$  - 2 d6

36  $\mu\text{l}$   $\text{H}_3\text{PO}_4$

1 ml

0.56 ml of sol + 0.44 ml of  $\text{H}_2\text{O}$   
 $\approx$  1 ml solut.on

Deoxyadenosine H<sub>2</sub>O ~10 mg / ml

Paper: 0.32182 gm.

With powder: 0.34382

$$\begin{array}{r} -0.32182 \\ \hline 0.02200 \text{ gm} \end{array}$$

Add 2.2 ml.

~~(Candy)~~ ~~SOP 2~~  
~~CBR~~

2-deoxy-D-ribose ~ 10 mg / ml.

Paper: 0.33946

Add ~ 0.02 gm.

Nernst base: 0.35807

$$\begin{array}{r} -0.33946 \\ \hline 0.01861 \text{ gm} \end{array}$$

Add ~ 1.9 ml.

Add  $\sim$  10 mg  $\rightarrow$  0.35164 gm

Actual amount 0.35836

$$\begin{array}{r} -0.35164 \\ \hline 0.01672 \text{ gm.} \end{array}$$

$\therefore \sim 1.67 \text{ ml H}_2\text{O for } 10 \text{ mg/1 ml.}$

---

DL-glyceraldehyde:  $\text{CH}_2\text{O} + \text{CHOH} \rightleftharpoons \text{CH}_2\text{O}$

25  $\mu$ g. Very soluble

Parch paper: 0.32332 gm.

[Add 0.00003 gm - scale too inaccurate]

W. glyceraldehyde 0.32353

$$\begin{array}{r} -0.32332 \\ \hline 0.00021 = 210 \mu\text{g.} \end{array}$$

in 2.1 ml water.

Solubility:  $\beta$ -D-glucose, M.W. 180.2  
 $\beta$  has 154 at  $15^{\circ}\text{C}$  in  $\text{H}_2\text{O}$

$$\text{i.e., } 154 \text{ gm/l} / 100 \text{ ml} = 1.54 \text{ gm/ml.}$$

$$\therefore 10^{-3} \text{ gm requires } \frac{10^{-3}}{1.54} \approx 0.6 \times 10^{-3} = 6 \times 10^{-4} \text{ ml}$$

for saturated sol.

Ruth Marin says 10 mg/ml for glucose standard.  
that 100 µg gives good color definition on paper.

Powder  
Paper: 0.34164 gm.

~~also ~10 mg ~0.01 gm — 0.3400~~

~~Actual amt : 0.34548 gm~~

$$\begin{array}{r} 0.34164 \\ \hline 0.00384 \\ \hline 3.84 \text{ mg } \beta\text{-D glucose} \end{array}$$

## Small Hood

Büchi Evaporators (2), Glasapparatefabrik Flaw, I  
+ assorted evaporation flasks + heavy ringstand bases.

## Blotting Paper

Radioactive waste disposal bin; ordinarily for  
sub milliecurie range.

Disposable pipettes + rubber bulbs

Massline Non-woven towels.

Ultrasonic cleaner: Acoustica Associates, Inc.,  
Mineola, N.Y. Model DR 252

Sterilmaster small autoclave.

## Sinks

Lakeside Mfg. Inc., Milwaukee 7, Wisc.

Wheeled push cart <sup>Model</sup> No. 526.

2 2000 ml <sup>cylindrical</sup> graduates, stoppered; 2/500 ml.

Assorted 1.5 to 2 l. stoppered bottles

Marking crayons

Electric sockets on benches for hairdryers + evaporators.

*N* Butanol: Formic Acid: Water, 77:10:13

adenine deoxyadenosine standard

+ 2. adenine-deoxyribose-phosphoric acid runs

→ ~ 1500 ml in stoppered graduate.

*N* Butanol:  $770 + 385 = 1155 \text{ ml}$

Formic Acid:  $100 + 50 = 150 \text{ ml}$

Water:  $130 + 65 = \frac{195 \text{ ml}}{1500 \text{ ml}}$  ✓

Solvent solution must be made up fresh.

↑ a tendency to decay, if used > after  
days after being mixed.

Micropipettes + syringes from Research  
Specialties Co., Model 1850

1000 ml Erlenmeyer

100 ml Narrow-necked Florence

Pipette Syringes: Instrumentation Associates, N.Y.

Kenmore Hair Dryers, Model 559-8710.

Khorana "Some recent developments  
in the chemistry of phosphate esters  
of biological interest," Wiley, 1961

Sudan Black is a solvent front marker.

Succic acid used as shadowing development stop.  
Kodagraph developer, Kodate fixer.  
Kodagraph Contact Standard.

A Manual of Paper Chromatography  
+ Paper Electrophoresis

- R. Block, F. L. Durrum, + G. Zway

2nd ed., 1958

Academic Press

Uv exposure box:

front side  
19" x 16" x 12" (depth)

Vycor glass sheet at top

Askey's Photo-Dry Model A-20X  
Electric Print Dryer

Timers

Wratten Series 6B filters for Uv lighting.

Drymaster X-ray Film Dryer, R-P Corporation

Picker X-ray  
RK.

Universal Aerosol Spray Kit  
Nutritional Biochem Corp., Cleveland

Analine - hydrogen phthalate spray for sugar.

Nos. Carolina Co., Portland, Ore.  
Chromatograph oven

a)      Y  
      Y

b)      Y  
      Y

2)

Y

Standards.

a) 10  $\mu$  Adenine + 10  $\mu$  ~~D~~ Deoxyadenosine

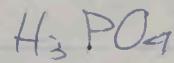
b) 10  $\mu$   $^{\beta}$ -D Glucose, 20  $\mu$  DL glyceraldhyde,  
20  $\mu$  2-Oxy-D-ribose

Refrigerate overnight

F<sub>as</sub> uv

①

Stoichiometric  
proportions



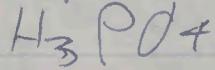
0.56mL sol. +

~~0.44mL~~ H<sub>2</sub>O

②

Min. Ac. Sol.

proportion



0.56mL sol. +

0.44mL 0.01M H<sub>3</sub>PO<sub>4</sub>

Tall

V<sub>y</sub> cor

Short

V<sub>y</sub> cor

Irradiation Began at 3:55 P.M.

We've diluted so I enough volume (~1mL) to  
efficiently irradiate. Tomorrow we must  
evaporate so sol. is concentrated enough  
to make a few mL of I spotting efficient.

~ 35 ml (trough of solvent permits  
chromatographs to be run overnight)

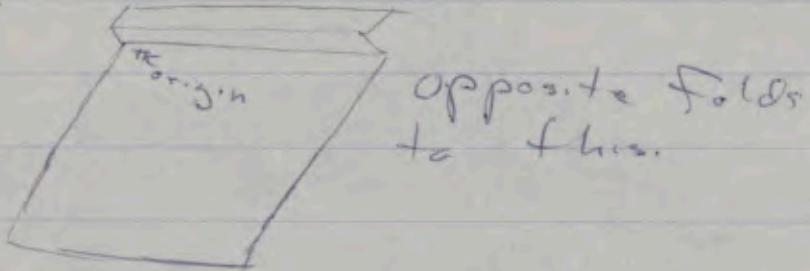
No. ① chromatogram, w. 2 x's on

No. ② " , w. 2 holes in

Glass square 3" + 3" (approx.)

Rubber glove

Fold paper



End Windsor Counter - Nuclear Chicago Model 186A.  
with Model T1 Dual Timer.

Gas handling manifold and compressed gases.

Chromatography chambers cost ~\$600.00 to  
build; sell at Richmond (or Bullock's) for  
~\$1,000.00. They are, in this form, ~~portable~~.

Glass still

"Data for Biochemical Research" - R.M.C.

Pawson, D.C. Elliott, W.H. Elliott, K.N. Jones  
Oxford U.P., 1959.

+  
+

- 1000 sheet boxes of Powder paper (glassine)  
 $3\frac{1}{2}'' \times 4\frac{1}{2}''$  No. 4, El. Lilly + Co., Indianapolis,  
A X - 29814 - A.
- Mottler Instrument Corp., Hightstown, N.J.  
Balance.
- Distilled water siphon, cork - surrounded, in  
Florence flask.
- Laboratory benches - dry - am't draws, etc.
- 5, 10, 20 ml beakers.
- Chromic trioxide for cleaning apparatus, etc.

Cat-aldehyde note: redistilled  $\text{CH}_3\text{CHO}$   
keeps indefinitely in 2M aqueous solution  
at  $-30^\circ$ . Dilute solns keep in cold at  
least a week. Polymerizes readily at  
any temp (Davson et al., p. 29)  $\mu_{\text{CH}_3\text{CHO}} = 14$   
 $= \mu_{\text{CO}_2}$  -- if  $\exists$  a physical reason for  $\text{CH}_3\text{CHO}$   
restricted to the oven, also must  $\exists \text{CO}_2$

Note 3 glycoaldehyde  $\text{CH}_3\text{OHCHO}$

1. Recipes for chromatography solvent systems
2. " " elution "
3. Reactions by heating spot in air to dry?
4. Function of oxalic acid

Pickar X-ray developing tank, 3 chambers  
+ water bath; <sup>45 min</sup> developer, wash; 5 min fix, 5 min  
hypoclearing agent, wash.  
Dry in oven  $\sim 15^{\text{m}}$ .

Shishongram: <sup>diluted</sup> Kodagraph developer (powder)  $\sim$  few sec's  
 $\sim 10^{\text{m}}$  sol. Acetic acid stop bath  $\sim$  few sec's  
diluted Kodak fixer (powder)  $\sim 5$  min  
4:11 dilutor Hypo clearing agent  $\sim 5$  min  
Wash  $\sim 5$  min  
Dry in  
Arkey Photo-dry  
Model A-20 A  
Electric print dryer

Paper ③ : 0.35013 gm.

added adrenin makes 0.35167 gm.

$$\therefore \text{amt adrenin} = \frac{0.35167 - 0.35013}{0.00154} \text{ gm} \approx 1.54 \text{ mg.}$$

$$1.54 \text{ mg responses } \frac{1.54}{1.69} = 1.69 \text{ ml}$$

## Standards preparation protocol

We desire 1 mg standard / ml. solvent (usually water). If standard I is entirely soluble in water we mix 1 mg w. 1 ml H<sub>2</sub>O. Otherwise we add more water, weighted as the solubility, a quantity found - Dawson et al.

The standard is weighed on a microbalance by difference methods. First weigh a piece of powder paper; then add the 1 mg or so of standard on the paper inside the balance chamber. Balance is sensitive to hand on table, the walking of passersby etc. Powder is removed by spatulas, mixed w. water in glass vials. Water amt is measured by pipettes w. graduated scales. Vials have screw tops.

Solubility in gm solute dissolving in 100 ml solvent.

adenine: 0.09 at 25 °C.

$$0.09 \text{ gm / 100 ml} = \frac{9 \times 10^{-2} \text{ gm}}{10^2 \text{ ml}} = 9 \times 10^{-4} \text{ gm / ml.}$$
$$\therefore 10^{-3} \text{ gm requires } \frac{10^{-3}}{9 \times 10^{-4}} = 0.11 \times 10 = 1.1 \text{ ml.}$$

Just as Cyril says,  $\sim$  1 mg / ml.

Paper weighing:

Paper ① 0.3615 gm

Paper ② 0.34238 gm.

We use paper ②. We want 1 mg = 0.001 gm adenine.  
∴ paper will weigh 0.3434 gm w. adenine.

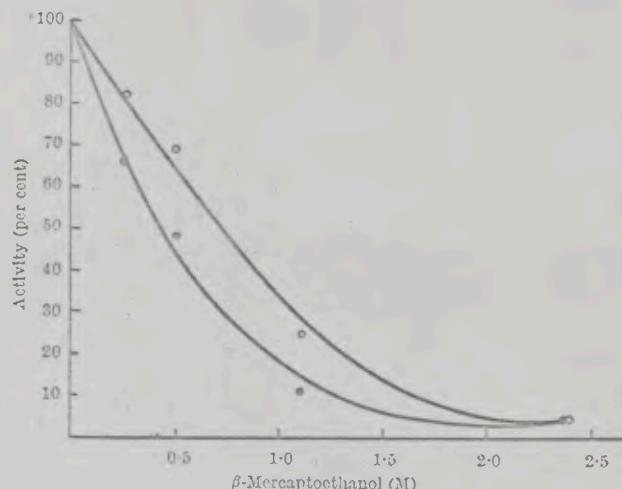


Fig. 4. Percentage enzymatic activity of crystalline pig heart LDH₂ (○) and rabbit muscle LDH₂ (●) isozymes after inhibition with  $\beta$ -mercaptoethanol at the concentrations indicated. Pyruvate was used as substrate.

homogenates in normal human serum in order to simulate more closely the situation which arises in myocardial infarction. In these experiments it was verified, by calculation on the base of data observed with homogenates alone, that the degree of denaturation by urea in the serum corresponded with that received. Our observations of denaturation with 1.5 M urea in the conditions described indicate that this technique would be useful for separating the monomers occurring preponderantly in the heart tissue from others for clinical purposes; certainly the test described is simple to carry out.

After we had prepared our communication, Hardy (*Nature*, 206, 933; 1965) published work concerning the denaturation of LDH of human and liver homogenates by urea. The concentration used by him was higher (2.6 M). At this concentration our curves show nearly complete denaturation of all isozymes studied. This difference might well be due to the shorter incubation period used by him. Also the fact that the co-enzyme was added to the incubation solution may contribute to differences in the results.

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#### Ultra-violet Spectroscopy in the Analysis of Chromatograms

THE sensitivity of the normal human eye to light does not extend far below 400 m $\mu$ . Nevertheless, ultra-violet-absorbing compounds appear as dark spots on paper chromatograms illuminated with ultra-violet light. This is due to absorption of the light before it can excite the fluorescence of the paper, and constitutes one variety of quenching. Compounds which fluoresce in ultra-violet light will be detected on paper chromatograms if their

fluorescence exceeds that of the surrounding paper. The light sources commonly employed emit the mercury lines at 254 m $\mu$  or 366 m $\mu$ . In chromatograms of biological extracts the short-wave lamp detects principally the absorbing compounds and the long-wave lamp fluorescing compounds. Beyond this the method possesses little inherent specificity. Thus compounds such as cortisone, nicotinic acid, caffeine and uric acid ( $\lambda_{\text{max}}$  240, 260, 273 and 292 m $\mu$  respectively) all appear indistinguishable as dark spots under the short-wave lamp. Furthermore, for substances such as oestrogens, the absorption maximum (280 m $\mu$ ) of which is very different from the 254 m $\mu$  emission of the handlamp, the method is relatively insensitive. A need therefore exists for an instrument with which absorption and activation maxima can be rapidly determined on the paper. I have accordingly designed an ultra-violet spectroscope in which the ultra-violet light is shifted to the visible region by the fluorescence of either the paper itself or a superimposed screen.

The light source, an 'Osram' 450-W xenon arc, provides an ultra-violet continuum. After passing through a quartz prism monochromator (Schaeffel Instrument Co., Westwood, N.J.) with variable exit slit, the light emerges through a  $1\frac{1}{16} \times \frac{3}{8}$  in. rectangular aperture as a slightly divergent beam which illuminates the chromatogram. The latter is attached by spring clips to a frame, which can be moved manually in three planes, or by a motor in the direction of solvent flow only. A screen coated with a suitable phosphor can be placed in position over the illuminated portion of the chromatogram if desired. Among several phosphors examined,  $\text{ZnSiO}_4 : \text{Mn}$  and  $(\text{Sr}, \text{Mg})_3(\text{PO}_4)_2 : \text{Sn}$  were found to be the most generally useful. The former is slightly phosphorescent, but not excessively so. It provides a bright illumination over the range 230–295 m $\mu$  and 330–400 m $\mu$ . The latter exhibits a continuous though less intense fluorescence over the range 230–370 m $\mu$ , and is therefore suitable for rapid, routine searching. To obtain linear wave-length drive the prism is rotated by means of a cam, which is attached to a digital counter. The optical arrangement is shown in Fig. 1, and the assembled apparatus in Fig. 2.

In order to make a visual estimate of the absorption maximum of a compound on a chromatogram, the wave-length knob is rotated until the spot is darkest. The fluorescent screen may be needed to provide adequate background illumination. With certain compounds the maximum is best approached from higher wave-lengths, as the absorption does not always fall off as sharply below the maximum. It is desirable that the brightness of the paper or screen should remain constant while the wave-length of the incident light is varied. To accomplish this a second cam can be used to vary the slit width at different wave-lengths, so as to compensate for changes in the output of the xenon arc, the dispersion of the monochromator, and the spectral response of the paper or screen phosphor.

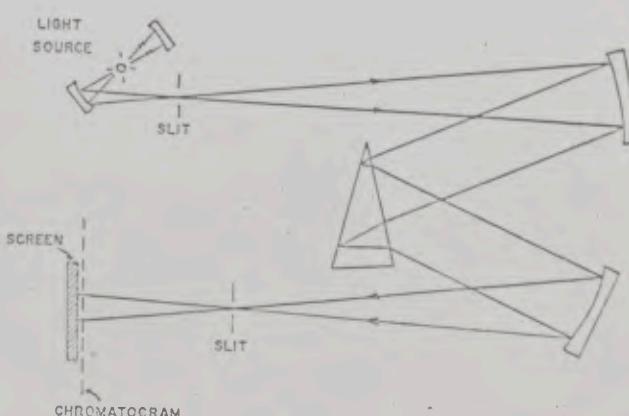


Fig. 1. Optical arrangement of the ultra-violet spectroscope

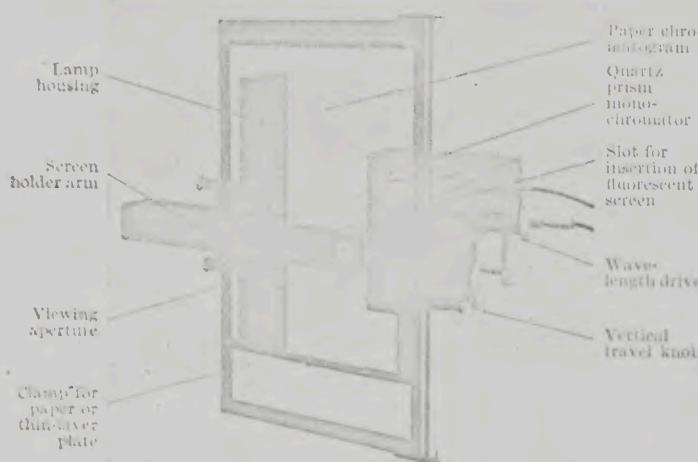


Fig. 2. The assembled spectroscope

If 'Kodabromide F5' or other suitable photographic paper<sup>1</sup> is placed in contact with the chromatogram, a record of absorbing or fluorescing<sup>2</sup> compounds can be obtained at any desired wave-length within the operating range of the instrument. If the entire strip is to be photographed the rectangular aperture is replaced by a narrow slit, past which the paper is drawn either by hand or by means of a motor. Arnold *et al.*<sup>3</sup> described a similar arrangement for photographing chromatograms, but they used a mercury source, which would only be suitable for observations at certain wave-lengths.

For the determination of the activation spectrum of a fluorescent compound the screen is best avoided, as its fluorescence may mask that of the compound under study. The wave-length knob is rotated until maximal fluorescence is produced. The point at which this occurs will differ slightly from the true activation maximum of the compound, because the intensity of the light issuing from the monochromator increases with wave-length (unless the slit is automatically adjusted by means of a cam). However, a reasonable approximation can be made.

Another application lies in the analysis of thin-layer chromatograms. For this purpose the addition of 10 per cent  $ZnSiO_4 : Mn$  to the solid phase converts the plate itself into a fluorescent screen. Better contrast is obtained with this technique than with the screen superimposed on a paper chromatogram, which absorbs a significant proportion of the incident light. It was found that quantities of oestrogens which were barely detectable under the 254 m $\mu$  handlamp could easily be seen with the spectroscope set at 280 m $\mu$ .

The foregoing description has chiefly been concerned with the analysis of compounds on chromatograms. Analogous results can be obtained with compounds in solution in quartz cuvettes. To facilitate the observation of small changes in optical density a reference cell containing the solvent alone is placed alongside the unknown solution. With the aid of the fluorescent screen, absorption maxima can be estimated in exactly the same way as on paper. For example, as little as 2  $\mu$ g cortisol in 1 ml. absolute ethanol could be spectrally analysed; and the end-absorption of absolute ethanol was discernible below 220 m $\mu$  in comparison with a reference cell containing water.

The apparatus can be adapted for automatic scanning of chromatographic strips at a given wave-length, or for recording the absorption spectra of compounds on chromatograms. Modifications of existing spectrophotometers for such purposes have been described by others<sup>4-6</sup>. The principal advantage of the present technique is that it provides a tool of high sensitivity, permitting the

spectral characteristics of compounds to be studied visually. Furthermore, areas which appear only as streaks on conventional ultra-violet illumination can often be shown by spectroscopy to contain several discrete spots with different absorption or activation maxima. In this way, full advantage can be taken of the high resolving power of the paper or thin-layer chromatogram. These developments have been made possible by the availability of sufficiently intense sources emitting a continuous spectrum in the ultra-violet region.

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### Accumulation and Incorporation of Amino-acid in Rat Intestine *in vitro*

INVESTIGATIONS of the absorption of amino-acids from the intestinal tract have usually been concerned with a single amino-acid or, in some cases, simple mixtures of a few amino-acids<sup>1-3</sup>. Under physiological conditions, on the other hand, an initial stage in the assimilation of dietary proteins is the enzymatic liberation during digestion of a mixture composed of peptides and 18-20 free amino-acids<sup>4</sup>. Because of the interactions between the amino-acids in competing for several relatively specific transfer mechanisms, the total rate of absorption of amino-acids from a mixture need not be closely related to the absorption rates of the same amino-acids when measured singly, but will depend on the composition of the mixture present in the intestinal lumen<sup>4</sup>. There is also evidence that during absorption for 1 h of glycine *in vitro*<sup>5</sup> and of protein hydrolysate *in vitro*<sup>6</sup> there is an incorporation of the absorbed amino-acids into the protein of rat intestinal mucosal cells. This communication records an investigation of amino-acid transport and protein synthesis in rat intestine during absorption of an amino-acid mixture *in vitro*.

Amino-acid transport was measured over 8 min as the entry of <sup>14</sup>C-labelled amino-acids into the tissue water and proteins of rings of jejunum prepared from male albino rats ranging in weight from 260 to 300 g. The rings<sup>7</sup> (2-5 mg dry weight) were incubated in 2.5 ml. of medium containing a mixture of 18 amino-acids giving a total amino-acid concentration of 1.7 mM, and containing 0.4  $\mu$ c. of a <sup>14</sup>C-labelled protein hydrolysate ('CFB 25', Radiochemical Centre, Amersham). The incubations were terminated by the addition of an excess of an unlabelled casein hydrolysate and the rings rapidly removed from the medium, blotted, and transferred to 3 ml. 0.5 M perchloric acid at 0.5° C. The tissue was dispersed with a glass rod and the precipitated protein removed by centrifugation. An aliquot of the supernatant was counted to give a measure of the amount of labelled material in the perchloric acid extract. A correction was made for the carry-over of label from the medium by counting similar aliquots of perchloric acid extracts of rings incubated for 15 sec in a medium identical except for the presence of the excess of unlabelled casein hydrolysate. Apart from this correction no attempt was made to allow for the extracellular space or for any non-absorbing tissue present in the rings. If such corrections were made, the ratio of the concentration of amino-acids in the tissue fluid to that in the medium (T/M) would tend to increase when the ratio was greater than 1.

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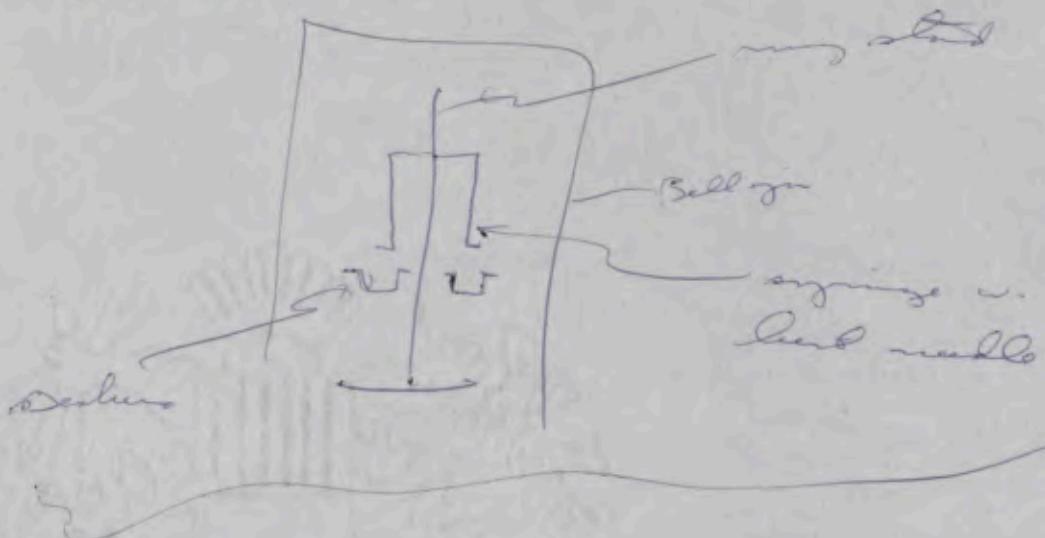
401 B'Dwyer

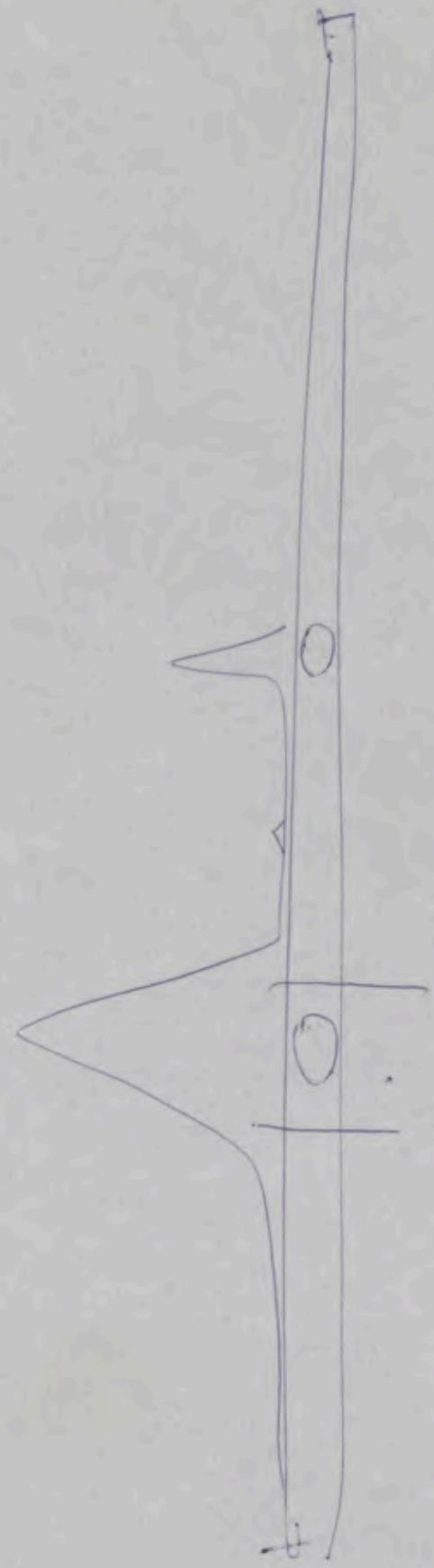
N.Y. 13, N.Y.

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Electro





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Cyl will provide window for end-mica center.  
Gold-coated mylar.

Egypt will give  
blueprints for their cols.